



Lecture 11

Programming Shared Memory III

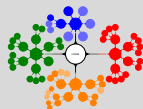
OpenMP (Open Multi-Processing); Parallelization Application
Example - Pi Computation

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1 Parallelization Application Example-OpenMP Computing π



Computing π I

Computing π using Sequential Code

An OpenMP version of a threaded program to compute π number using random numbers.

Computing π using OpenMP directives - Random Numbers.

Follow the steps below for executing OpenMP code;

```
gcc -o code21 code21.c -fopenmp
./code21
```

```
1  /*****
2  An OpenMP version of a threaded program to compute PI.
3  *****/
4  #pragma omp parallel default(none) private(rand_no_x, rand_no_y,
5     num_threads, sample_points_per_thread) shared(npoints)
6     reduction(+: sum) num_threads(8)
7     {
8         num_threads = omp_get_num_threads();
9         sample_points_per_thread = npoints / num_threads;
10
11        sum = 0;
12        for (int i = 0; i < sample_points_per_thread; i++) {
13            rand_no_x = (double)rand() / (double)RAND_MAX;
14            rand_no_y = (double)rand() / (double)RAND_MAX;
15            if (((rand_no_x - 0.5) * (rand_no_x - 0.5) + (
16                rand_no_y - 0.5) * (rand_no_y - 0.5)) < 0.25) {
17                sum = sum + 1;
18            }
19        }
20    }
```

- Note that this program is much easier to write in terms of specifying creation and termination of threads compared to the corresponding POSIX threaded program.
- The `omp_get_num_threads()` function returns the number of threads in the parallel region
- The `omp_get_thread_num()` function returns the integer id of each thread (recall that the master thread has an id 0).
- The *parallel directive* specifies that all variables except *npoints*, the total number of random points in two dimensions across all threads, are local.
- Furthermore, the directive specifies that there are eight threads, and the value of sum after all threads complete execution is the sum of local values at each thread.
- A for loop generates the required number of random points (in two dimensions) and determines how many of them are within the prescribed circle of unit diameter.



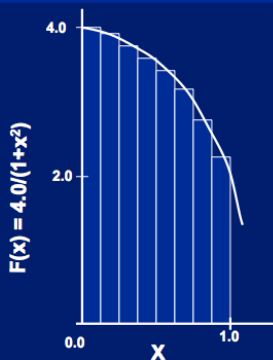
Computing π III

An OpenMP version of a threaded program to compute PI number by numerical integration without reduction clause.

Computing PI using OpenMP directives -
Numerical Integration. Follow the steps below;

```
export OMP_NUM_THREADS=4
gcc -o code22 code22.c -fopenmp
./code22
```

Numerical Integration



Mathematically, we know that:

$$\int_0^1 \frac{4.0}{(1+x^2)} dx = \pi$$

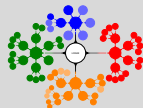
We can approximate the integral as a sum of rectangles:

$$\sum_{i=0}^N F(x_i) \Delta x \approx \pi$$

Where each rectangle has width Δx and height $F(x_i)$ at the middle of interval i .

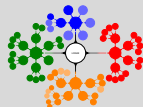


Computing π IV - Sequential Calculation



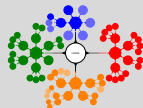
```
1 #include <stdio.h>
2 #include <math.h>
3 int main(int argc, char* argv[])
4 {
5     int done = 0, n, i;
6     double PI25DT = 3.141592653589793238462643;
7     double mypi, h, sum, x;
8     while (!done)
9     {
10        printf("Enter the number of intervals: (0 quits) ");
11        scanf("%d",&n);
12
13        if (n == 0) break; /* Quit when "0" entered*/
14        /* Integral limits are from 0 to 1 */
15        h = (1.0-0.0)/(double)n; /* Step length*/
16        sum = 0.0; /* Initialize sum variable */
17        for (i = 1; i <= n; i += 1) /* loop over interval for
18        integration */
19        {
20            x = h * ((double)i - 0.5); /* Middle point at step */
21            sum += 4.0 / (1.0 + x*x); /* Sum up at each step */
22            // printf("i=%d x=%f sum=%f \n",i,x,sum); /* print
23            intermediate steps */
24        }
25        mypi = h * sum; /* Obtain resulting pi number */
26        printf("pi is approximately %.16f, Error is %.16f\n",mypi,
27        fabs(mypi - PI25DT));
28    }
29 }
```

Computing π IV - OpenMP Parallel Calculation



```
1 #include <stdio.h>
2 #include <math.h>
3 #include <omp.h>
4 #define NUM_THREADS 4
5
6 int main(int argc, char* argv[])
7 {
8     int done = 0, n, i;
9     double PI25DT = 3.141592653589793238462643;
10    double mypi, h, sum[NUM_THREADS], x;
11
12    while (!done)
13    {
14        printf("Enter the number of intervals: (0 quits) ");
15        scanf("%d",&n);
16
17        if (n == 0) break; /* Quit when "0" entered */
18        /* Integral limits are from 0 to 1 */
19        h = (1.0-0.0)/(double)n; /* Step length */
20        #pragma omp parallel private ( i, x )
21        {
22            int id = omp_get_thread_num();
23            sum[id]=0.0; /* Initialize sum variable */
24            for ( i = id+1; i <= n; i += NUM_THREADS) /* loop over interval for integration */
25            {
26                x = h * ((double)i - 0.5); /* Middle point at step */
27                sum[id] += 4.0 / (1.0 + x*x); /* Sum up at each step */
28            }
29        }
30        for(i=1; i<NUM_THREADS; i++)
31            sum[0] += sum[i];
32        mypi = h * sum[0]; /* Obtain resulting pi number */
33        printf("pi is approximately %.16f, Error is %.16f\n",mypi, fabs(mypi - PI25DT));
34    }
35 }
```

Computing π V - OpenMP Parallel Calculation



Access to Sequential Code & OpenMP Parallel Code

```
gcc -o sequential_pi sequential_pi.c
./sequential_pi
Enter the number of intervals: (0 quits) 100
pi is approximately 3.1416009869231254, Error is 0.0000083333333323
Enter the number of intervals: (0 quits) 1000
pi is approximately 3.1415927369231227, Error is 0.000000833333296
Enter the number of intervals: (0 quits) 10000
pi is approximately 3.1415926544231341, Error is 0.000000008333410
Enter the number of intervals: (0 quits) 0
```

```
gcc -o parallel_OpenMP_pi parallel_OpenMP_pi.c -fopenmp
./parallel_OpenMP_pi
Enter the number of intervals: (0 quits) 100
pi is approximately 3.1416009869231249, Error is 0.0000083333333318
Enter the number of intervals: (0 quits) 1000
pi is approximately 3.1415927369231267, Error is 0.0000008333333336
Enter the number of intervals: (0 quits) 10000
pi is approximately 3.1415926544231239, Error is 0.000000008333307
Enter the number of intervals: (0 quits) 0
```

Table: Sequential and OpenMP outputs for computing π number.

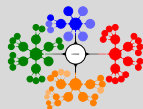


An OpenMP version of a threaded program to compute PI number by numerical integration with reduction clause.

Computing PI using OpenMP directives - **Reduction**. Follow the steps below for executing OpenMP code;

```
export OMP_NUM_THREADS=8  
gcc -o code23 code23.c -fopenmp  
./code23
```

Computing π VII - OpenMP Parallel Calculation: Reduction



```
1 #include <stdio.h>
2 #include <math.h>
3 #include <omp.h>
4 int main(int argc, char* argv[])
5 {
6     int done = 0, n, i;
7     double PI25DT = 3.141592653589793238462643;
8     double mypi, h, sum, x;
9     while (!done)
10    {
11        printf("Enter the number of intervals: (0 quits) ");
12        scanf("%d",&n);
13        if (n == 0) break; /* Quit when "0" entered*/
14        /* Integral limits are from 0 to 1 */
15        h = (1.0-0.0)/(double)n; /* Step length*/
16        sum = 0.0; /* Initialize sum variable */
17        #pragma omp parallel for private(x) reduction (+:sum)
18        for (i = 1; i <= n; i += 1) /* loop over interval for
19            integration */
20        {
21            x = h * ((double)i - 0.5); /* Middle point at step*/
22            sum += 4.0 / (1.0 + x*x); /* Sum up at each step*/
23        }
24        mypi = h * sum; /* Obtain resulting pi number */
25        printf("pi is approximately %.16f, Error is %.16f\n",mypi,
26            fabs(mypi - PI25DT));
27    }
```