

MSE228 Engineering Quantum Mechanics
 Quiz 6 Duration: 30 minutes Open Book Quiz

1. (a) How many different sets of quantum numbers (n, l, m_l, m_s) are possible for an electron in the 4f level? (b) Suppose a certain atom has three electrons in the 4f level. What is the maximum possible value of the total m_s of the three electrons? (c) What is the maximum possible total m_l of three 4f electrons? (d) Suppose an atom has ten electrons in the 4f level. What is the maximum possible value of the total m_s of the ten 4f electrons? (e) What is the maximum possible total m_l of ten 4f electrons?

a) $4f \rightarrow n=4, l=3 \rightarrow m_l = +3, +2, +1, 0, -1, -2, -3$ & $m_s = +\frac{1}{2}, -\frac{1}{2} \Rightarrow 7 \times 2 = \boxed{14}$
7 possible combinations

b) Three $\bar{e}s \rightarrow 7 \bar{e}s$ can have state $m_s = +\frac{1}{2} \Rightarrow$ three $\bar{e}s$ $m_s = 3 \times \frac{1}{2} = \boxed{+\frac{3}{2}}$

c) $m_l = +3 \rightarrow m_s = +\frac{1}{2}$ & $m_l = +2 \rightarrow m_s = +\frac{1}{2} \Rightarrow 2 \times (+3) + 1 \times (+2) = \boxed{+8}$
 $\rightarrow m_s = -\frac{1}{2}$

d) Ten $\bar{e}s \rightarrow 7 \bar{e}s$ can have state $m_s = +\frac{1}{2}$ & 3 $\bar{e}s$ can have state $m_s = -\frac{1}{2}$
 $\Rightarrow 7 \times (+\frac{1}{2}) + 3 \times (-\frac{1}{2}) = \boxed{2}$

e) $m_l = +3 \rightarrow m_s = +\frac{1}{2}$ & $m_l = +2 \rightarrow m_s = +\frac{1}{2}$ & $m_l = +1 \rightarrow m_s = +\frac{1}{2}$ & $m_l = 0 \rightarrow m_s = +\frac{1}{2}$ & $m_l = -1 \rightarrow m_s = +\frac{1}{2}$
 $\rightarrow m_s = -\frac{1}{2}$

$10 \bar{e}s = 2 + 2 + 2 + 2 + 2$
 $\Rightarrow 2 \times (+3) + 2 \times (+2) + 2 \times (+1) + 2 \times (0) + 2 \times (-1) = \boxed{10}$

2. (a) The ionization energy of sodium is 5.14 eV. What is the effective charge seen by the outer electron? (b) If the 3s electron of a sodium atom is moved to the 4f state, the measured binding energy is 0.85 eV. What is the effective charge seen by an electron in this state?

$$E_n = Z_{\text{eff}}^2 \frac{E_1}{n^2}, \text{ where } E_1 = -13.6 \text{ eV}$$

a) $3s, E_3 = -5.14 \text{ eV} \rightarrow Z_{\text{eff}} = n \sqrt{\frac{E_3}{-13.6 \text{ eV}}} = 3 \sqrt{\frac{-5.14 \text{ eV}}{-13.6 \text{ eV}}} = \boxed{1.84}$

Na: $1s^2 2s^2 2p^6 3s^1$, 11(+e) in nucleus } $1 = Z_{\text{eff}}$: expected
 10(-e) in core $\bar{e}s$

So, less screened by the inner $\bar{e}s$. 3s electron is penetrating the inner orbit.

b) $4f, E_4 = -0.85 \text{ eV} \rightarrow Z_{\text{eff}} = 4 \sqrt{\frac{-0.85 \text{ eV}}{-13.6 \text{ eV}}} = \boxed{1.00}$

so, screening is complete.