



İzmir Kâtip Çelebi University
Department of Engineering Sciences
Phy101 Physics I
Midterm Examination
April 04, 2022 08:30 – 10:00
Good Luck!

NAME-SURNAME:

SIGNATURE:

ID:

DEPARTMENT:

INSTRUCTOR:

DURATION: 90 minutes

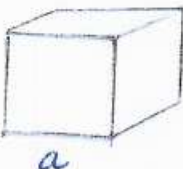
- ◇ Answer all the questions.
- ◇ Write the solutions explicitly and clearly.
Use the physical terminology.
- ◇ You are allowed to use Formulae Sheet.
- ◇ Calculator is allowed.
- ◇ You are not allowed to use any other electronic equipment in the exam.

Question	Grade	Out of
1A		15
1B		10
1C		10
2		20
3		20
4		20
5		20
TOTAL		115

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1. A) The side of a cube of metal is measured to be (1.60 ± 0.05) cm and its mass is measured to be (30.1 ± 0.4) g
- Find the perimeter of one face of the cube with the uncertainty.
 - Find the volume and uncertainty in the volume.
 - Determine the density of the solid in kilograms per cubic meter and the uncertainty in the density.

You should be using the correct number of significant figures in your result.



$a = (1.60 \pm 0.05) \text{ cm} = (1.60 \pm 0.05) \times 10^{-2} \text{ m}$
 $m = (30.1 \pm 0.4) \text{ g} = (30.1 \pm 0.4) \times 10^{-3} \text{ kg}$
 $\leadsto 3 \text{ sig figs} //$

i) Perimeter: $4a = 4(1.60 \pm 0.05) \times 10^{-2} \text{ m} = (6.40 \pm 0.20) \times 10^{-2} \text{ m}$

ii) volume: $V = a^3 \leadsto C = A^n, \Delta C = C/n \frac{\Delta A}{A}$

$\Rightarrow V = a^3 = (1.60 \times 10^{-2} \text{ m})^3 = 4.10 \times 10^{-6} \text{ m}^3$
 $\Delta V = a^3 / 3 \frac{\Delta a}{a} = 4.10 \times 10^{-6} / 3 \frac{0.05}{1.60} = 0.38 \times 10^{-6} \text{ m}^3$
 $\Rightarrow \text{Volume} = (4.10 \pm 0.38) \times 10^{-6} \text{ m}^3$

iii) density: $\rho = m/V \leadsto C = \frac{A}{B}, \Delta C = |C| \sqrt{\left(\frac{\Delta A}{A}\right)^2 + \left(\frac{\Delta B}{B}\right)^2}$

$\rho = \frac{m}{V} = \frac{30.1 \times 10^{-3} \text{ kg}}{4.10 \times 10^{-6} \text{ m}^3} = 7341 \text{ kg/m}^3 \sim 734 \times 10^3 \text{ kg/m}^3$
 $\Delta \rho = \left| \frac{30.1 \times 10^{-3} \text{ kg}}{4.10 \times 10^{-6} \text{ m}^3} \right| \sqrt{\left(\frac{0.4}{30.1}\right)^2 + \left(\frac{0.38}{4.10}\right)^2} = 687 \text{ kg/m}^3$
 $\Rightarrow \text{density: } \rho = (7.34 \pm 0.69) \times 10^3 \text{ kg/m}^3$ Results in 3 sig figs

- B) The position of a particle moving along an x -axis is given by $x(t) = 12t^2 - 2t^3$, where x is in meters and t is in seconds.
- Determine the acceleration of the particle at $t = 3.0$ s.
 - What are the maximum positive coordinate reached by the particle and the acceleration of the particle at that instant?

i) $x(t) = 12t^2 - 2t^3$

$$v(t) = \frac{dx}{dt} = 24t - 6t^2 \quad (1)$$

$$a(t) = \frac{dv}{dt} = 24 - 12t \quad (1) \rightarrow a(t=3s) = 24 - 12 \times 3 = \underline{\underline{-12 \text{ m/s}^2}} \quad (1) \quad (1)$$

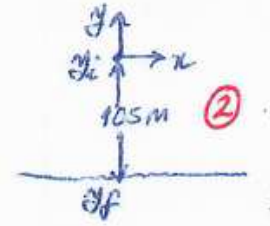
ii) maximum positive coordinate $\Rightarrow v(t) = \frac{dx}{dt} = 0 \quad (2)$

$$24t - 6t^2 = 0 = 6t(4-t) = 0 \Rightarrow t = 4s \quad (1)$$

$$\rightarrow x(t=4s) = 12(4)^2 - 2(4)^3 = 192 - 128 = \underline{\underline{64m}}$$

$$a(t=4s) = 24 - 12 \times 4 = \underline{\underline{-24 \text{ m/s}^2}} \quad (1) \quad (1)$$

- C) A helicopter is ascending (move upward) vertically with a speed of 5.40 m/s. At a height of 105 m above the Earth, a package is dropped from the helicopter. How much time does it take for the package to reach the ground? [Hint: What is v_0 for the package?]



with our chosen coordinate system

$$v_0 = 5.40 \text{ m/s} \text{ as upward } \begin{cases} y_i = 105 \text{ m} \\ y_f = 0 \text{ m} \end{cases} \quad (2)$$

$$y_j - y_0 = v_0 t - \frac{1}{2} g t^2 \quad (2)$$

$$-105 - 0 = 5.4t - \frac{1}{2} 9.8 t^2 \Rightarrow 4.9t^2 - 5.4t - 105 = 0 \quad (2)$$

Quadratic equation

$$\Rightarrow t_{1,2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-(-5.4) \pm \sqrt{(-5.4)^2 - 4(4.9)(-105)}}{2 \times 4.9}$$

$$= \frac{5.4 \pm \sqrt{29.16 + 2059.2}}{9.8} = \frac{5.4 \pm 45.215}{9.8}$$

$5.215 \text{ s} \quad (2)$
 -4.115 s

2. Vectors \vec{A} and \vec{B} lie in an xy -plane. \vec{A} has magnitude 8.0 and an angle 130° ; B has components $B_x = -7.72$ and $B_y = -9.20$.

i) What are $5\vec{A} \cdot \vec{B}$ and $4\vec{A} \times 3\vec{B}$ in unit vector notation?

ii) What is $(3\hat{i} + 5\hat{j}) \times (4\vec{A} \times 3\vec{B})$? Find magnitude and angle of resultant vector.

\vec{A} & \vec{B} lie in xy -plane \Rightarrow only x & y components
 $|\vec{A}| = 8$ with angle 130° & $B_x = -7.72$, $B_y = -9.20$
 $\Rightarrow \vec{A} = |\vec{A}| \cos 130^\circ \hat{i} + |\vec{A}| \sin 130^\circ \hat{j} = \underline{-5.14 \hat{i} + 6.13 \hat{j}}$
 $\vec{B} = -7.72 \hat{i} + 9.20(-\hat{j}) //$

i) $5\vec{A} \cdot \vec{B} = 5(-5.14 \hat{i} + 6.13 \hat{j}) \cdot (-7.72 \hat{i} - 9.20 \hat{j})$
 $= 5 [(-5.14)(-7.72) + (6.13)(-9.20)] = \underline{-83.58}$

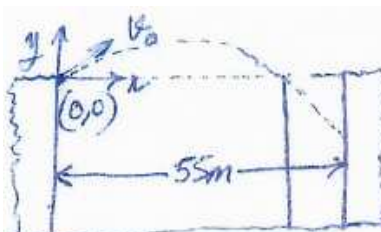
$4\vec{A} \times 3\vec{B} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ -20.56 & 24.52 & 0 \\ -23.16 & -27.6 & 0 \end{vmatrix} = \begin{matrix} (24.52 \times 0 - 0(-27.6)) \hat{i} \\ + (0(-23.16) - (-20.56)0) \hat{j} \\ + ((-20.56)(-27.6) - (24.52)(-23.16)) \hat{k} \end{matrix}$
 $= \underline{1135.4 \hat{k}}$

ii) $(3\hat{i} + 5\hat{j}) \times (1135.4 \hat{k}) = (3 \times 1135.4)(\hat{i} \times \hat{k}) + (5 \times 1135.4)(\hat{j} \times \hat{k})$
 $\hat{i} \rightarrow \hat{j} \rightarrow \hat{k}$
 $= 5677 \hat{i} + 3460.2(-\hat{j})$

Magnitude: $\sqrt{(5677)^2 + (-3460.2)^2} = \underline{6620.5}$
 angle: $\theta = \tan^{-1} \frac{-3460.2}{5677} = \underline{-31^\circ}$ or $\underline{329^\circ}$

3. A ball is shot from the top of a building with an initial velocity of 18 m/s at an angle $\theta = 42^\circ$ above the horizontal.

- i) What are the horizontal and vertical components of the initial velocity?
- ii) If a nearby building is the same height and 55 m away, how far below the top of the building will the ball strike the nearby building?



$v_0 = 18 \text{ m/s}$
 $\theta = 42^\circ$

i) $v_x = v_0 \cos \theta = 18 \text{ m/s} \cos 42 = 13.38 \text{ m/s}$ (3)
 $v_y = v_0 \sin \theta = 18 \text{ m/s} \sin 42 = 12.04 \text{ m/s}$ (3)

ii) $v_x = v_{0x}$ & $\Delta x = v_{0x} t \rightarrow$ time of flight (3)
 $t = \frac{\Delta x}{v_{0x}} = \frac{55 \text{ m}}{13.38 \text{ m/s}} = 4.11 \text{ s}$ (1)

same time interval for y direction & $y_0 = 0$ (2)

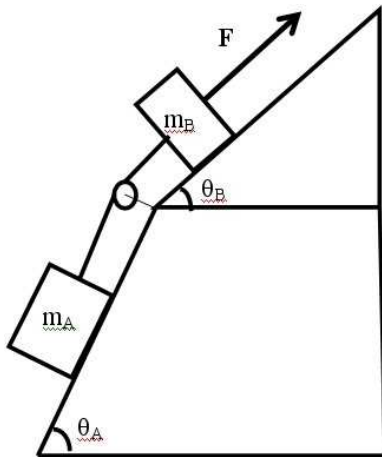
$$\Delta y = y - y_0 = v_{0y} t - \frac{1}{2} g t^2$$

$$= (12.04)(4.11) - \frac{1}{2} (9.8)(4.11)^2$$

$$= -33.3 \text{ m}$$

(2) (1) { minus sign shows below the top of the building

4. Consider the system shown in figure with $m_A = 9.5 \text{ kg}$ and $m_B = 11.5 \text{ kg}$. The angles $\theta_A = 59^\circ$ and $\theta_B = 32^\circ$.



- Draw the free body diagrams for block A and block B.
- In the absence of friction, what force F would be required to pull the masses at a **constant velocity** up?
- The force F now is removed. What is the magnitude and direction of acceleration of the two blocks?
- In the absence of F , what is the tension in the string?

i)

mass A
 ① x: $T - m_A g \sin \theta_A = m_A a_{Ax}$
 ② y: $F_N - m_A g \cos \theta_A = m_A a_{Ay}$

mass B
 ③ x: $F - T - m_B g \sin \theta_B = m_B a_{Bx}$
 ④ y: $F_N - m_B g \cos \theta_B = m_B a_{By}$

FBDs \rightarrow Newton's 2nd law
 \rightarrow equations of motion

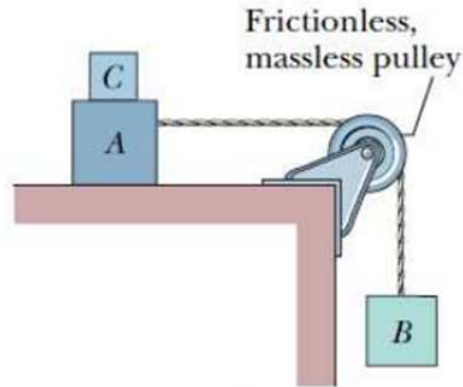
ii) constant velocity $\Rightarrow a = 0$ ① ② ③
 ① $T - m_A g \sin \theta_A = 0$
 ② $F - T - m_B g \sin \theta_B = 0$
 $\left. \begin{array}{l} \text{①} \\ \text{②} \end{array} \right\} F = T + m_B g \sin \theta_B$
 $= m_A g \sin \theta_A + m_B g \sin \theta_B$
 $= (9.5 \sin 59 + 11.5 \sin 32) \cdot 9.8 = 79.3 \text{ N} + 59.7 \text{ N} \approx 140 \text{ N}$

iii) now $a \neq 0$ ① ② ③
 ① $T - m_A g \sin \theta_A = m_A a$
 ② $F - T - m_B g \sin \theta_B = m_B a$
 $\left. \begin{array}{l} \text{①} \\ \text{②} \end{array} \right\} F = 0 \Rightarrow m_A (g \sin \theta_A + a) - m_B g \sin \theta_B = m_B a$
 $\Rightarrow a = \frac{-m_A g \sin \theta_A - m_B g \sin \theta_B}{m_A + m_B} = 6.7 \text{ m/s}^2 \text{ } (-\hat{i})$

iv) $T - m_A g \sin \theta_A = m_A a$ ③ $\sim T = m_A (a + g \sin \theta_A)$
 $= 9.5 (-6.7 + 9.8 \sin 59^\circ)$
 $\approx 16.2 \text{ N}$

5. In Figure, blocks A and B have weights of 44 N and 22 N, respectively.

- i) Determine the minimum weight of block C to keep A from sliding if μ_s between A and the table is 0.20.
- ii) Block C suddenly is lifted off A. What is the acceleration of block A if μ_k between A and the table is 0.15?



$m_A g = 44 \text{ N}$
 $m_B g = 22 \text{ N}$
 $\mu_s = 0.20$
 $\mu_k = 0.15$

Newton's 2nd law
A & C
 ① $T - f_s = m_A a_x = 0$
 ② $F_N - (m_A + m_C)g = m_{AC} a_y = 0$
B
 ③ $-T + m_B g = m_B a_y = 0$
 ④ $f_s = \mu_s F_N$

i) $m_C = ?$ if no motion
 $f_s = \mu_s F_N = \mu_s (m_A + m_C)g$

① $T - \mu_s (m_A + m_C)g = 0$
 ③ $T = m_B g$
 $\rightarrow W_{AC} = W_A + W_C = 110 \text{ N} \Rightarrow 44 \text{ N} + W_C = 110 \text{ N} \Rightarrow W_C = 66 \text{ N}$

ii) no m_C any more
 \Rightarrow motion now
 $\rightarrow \mu_k$

if sliding not to occur
 $T_B \leq T_{AC}$
 $W_B \leq \mu_s W_{AC}$
 $W_{AC} = \frac{22 \text{ N}}{0.20} = 110 \text{ N}$

① $T - \mu_k m_A g = m_A a$
 ② $F_N - m_A g = 0$
 ③ $-T + m_B g = m_B a$
 ④ $f_k = \mu_k F_N$

$$\frac{m_B g - \mu_k m_A g}{m_A + m_B} = a = \frac{22 \text{ N} - 0.15(44 \text{ N})}{(44 \text{ N} + 22 \text{ N})/9.8 \text{ m/s}^2}$$

$$a = 2.29 \text{ m/s}^2$$



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Department of Engineering Sciences
Phy101 Physics I
Canvas Midterm Examination
April 20, 2020 13:30
Good Luck!

NAME-SURNAME:

SIGNATURE:

ID:

DEPARTMENT:

DURATION: 180 minutes

- ◊ Solve 10 questions.
- ◊ Write the solutions explicitly and clearly.
- Use the physical terminology.

Question	Grade	Out of
TOTAL		110

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1. (Measurement) Calculate z and Δz for each of the following cases:

i $z = x - 2.5y + w$ for $x = (4.72 \pm 0.12) \text{ m}$, $y = (4.4 \pm 0.2) \text{ m}$,
 $w = (15.63 \pm 0.16) \text{ m}$.

ii $z = \frac{wx}{y}$ for $w = (14.42 \pm 0.03) \text{ m/s}^2$, $x = (3.61 \pm 0.18) \text{ m}$,
 $y = (650 \pm 20) \text{ m/s}$.

iii $z = x^3$ for $x = (3.55 \pm 0.15) \text{ m}$.

iv $z = A \sin y$ for $A = (1.602 \pm 0.007) \text{ m/s}$, $y = (0.774 \pm 0.003) \text{ rad}$.

Answer: i) $(9.4 \pm 0.5) \text{ m}$ ii) $(0.080 \pm 0.005) \text{ m/s}$ iii) $(44.7 \pm 5.7) \text{ m}^3$
 iv) $(1.120 \pm 0.006) \text{ m/s}$

i. $2.5y = 2.5(4.4 \pm 0.2) \text{ m} = (11 \pm 0.5) \text{ m}$

$$z = (4.72 - 11 + 15.63) \text{ m} = 9.35 \text{ m} \quad \Delta z = \sqrt{(0.12 \text{ m})^2 + (0.5 \text{ m})^2 + (0.16 \text{ m})^2}$$

$$= 0.539 \text{ m}$$

$$z \pm \Delta z = (9.4 \pm 0.5) \text{ m} \text{ (least precise)}$$

ii. $z = \frac{(14.42 \text{ m/s}^2)(3.61 \text{ m})}{650 \text{ m/s}} = 0.080 \text{ m/s}$ (2 sig. fig.)

$$\Delta z = |0.080 \text{ m/s}| \sqrt{\left(\frac{0.03 \text{ m/s}^2}{14.42 \text{ m/s}^2}\right)^2 + \left(\frac{0.18 \text{ m}}{3.61 \text{ m}}\right)^2 + \left(\frac{20 \text{ m/s}}{650 \text{ m/s}}\right)^2} = 0.00469 \text{ m/s}$$

$$z \pm \Delta z = (0.080 \pm 0.005) \text{ m/s}$$

iii. $z = (3.55 \text{ m})^3 = 44.7$ $\Delta z = |3.55 \text{ m}|^3$

$$\Delta z = (3.55 \text{ m})^3 \left| 3 \left(\frac{0.15 \text{ m}}{3.55 \text{ m}} \right) \right| = 5.671 \text{ m}^3$$

$$z \pm \Delta z = (44.7 \pm 5.7) \text{ m}^3$$

iv. $\sin y \pm (\cos y \Delta y) = \sin(0.774 \text{ rad}) \pm \cos(0.774 \text{ rad})(0.003 \text{ rad})$

$$z = (1.602 \text{ m/s})(0.699) = 1.11980 \text{ m/s}$$

$$\Delta z = (1.11980 \text{ m/s}) \sqrt{\left(\frac{0.002145}{0.699}\right)^2 + \left(\frac{0.007 \text{ m/s}}{1.602 \text{ m/s}}\right)^2} = 0.0059791 \text{ m/s}$$

$$z \pm \Delta z = (1.120 \pm 0.006) \text{ m/s}$$

2. (Measurement) The side of a cube of metal is measured to be (1.60 ± 0.05) cm and its mass is measured to be (30.1 ± 0.4) g

- i Find the perimeter of one face of the cube with the uncertainty.
- ii Find the volume and uncertainty in the volume.
- iii Determine the density of the solid in kilograms per cubic meter and the uncertainty in the density.

Answer: i) $4a = (6.40 \pm 0.20) \times 10^{-2}$ m ii) $V = (4.10 \pm 0.38) \times 10^{-6}$ m³
 iii) $\rho = (7.34 \pm 0.69) \times 10^3$ kg/m³

$a = (1.60 \pm 0.05) \text{ cm} = (1.60 \pm 0.05) \times 10^{-2} \text{ m}$
 $m = (30.1 \pm 0.4) \text{ g} = (30.1 \pm 0.4) \times 10^{-3} \text{ kg}$
 $\leadsto 3 \text{ sig figs} //$

i) perimeter: $4a = 4(1.60 \pm 0.05) \times 10^{-2} \text{ m} = (6.40 \pm 0.20) \times 10^{-2} \text{ m}$

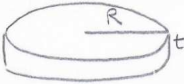
ii) volume: $V = a^3 \leadsto C = A^n, \Delta C = C/n \frac{\Delta A}{A}$
 $\Rightarrow V = a^3 = (1.60 \times 10^{-2} \text{ m})^3 = 4.10 \times 10^{-6} \text{ m}^3$
 $\Delta V = a^3 / 3 \frac{\Delta a}{a} = 4.10 \times 10^{-6} / 3 \frac{0.05}{1.60} = 0.38 \times 10^{-6} \text{ m}^3$
 $\Rightarrow \text{Volume} : (4.10 \pm 0.38) \times 10^{-6} \text{ m}^3$

iii) density: $\rho = m/V \leadsto C = \frac{A}{B}, \Delta C = |C| \sqrt{\left(\frac{\Delta A}{A}\right)^2 + \left(\frac{\Delta B}{B}\right)^2}$
 $\rho = \frac{m}{V} = \frac{30.1 \times 10^{-3} \text{ kg}}{4.10 \times 10^{-6} \text{ m}^3} = 7341 \text{ kg/m}^3 \sim 734 \times 10^3 \text{ kg/m}^3$
 $\Delta \rho = \left| \frac{30.1 \times 10^{-3} \text{ kg}}{4.10 \times 10^{-6} \text{ m}^3} \right| \sqrt{\left(\frac{0.4}{30.1}\right)^2 + \left(\frac{0.38}{4.10}\right)^2} = 687 \text{ kg/m}^3$
 $\Rightarrow \text{density} : \rho = (7.34 \pm 0.69) \times 10^3 \text{ kg/m}^3$ Results in 3 sig figs

3. (Measurement) A circular disk with a radius of (8.50 ± 0.02) cm and a thickness of (0.050 ± 0.005) cm.

- i Find the perimeter of the circle with the uncertainty.
- ii Find the volume and the uncertainty in the volume.

Answer: i) $2\pi R = (53.4 \pm 0.1) \times 10^{-2} \text{ m}$ ii) $V = (1.1 \pm 0.1) \times 10^{-5} \text{ m}^3$



$R = (8.50 \pm 0.02) \text{ cm} = (8.50 \pm 0.02) \times 10^{-2} \text{ m}$ (3sf)
 $t = (0.050 \pm 0.005) \text{ cm} = (0.050 \pm 0.005) \times 10^{-2} \text{ m}$ (2sf)

a) $2\pi R = 2\pi (8.50 \pm 0.02) \times 10^{-2}$
 $= (53.4 \pm 0.1) \times 10^{-2} \text{ m}$

b) $V = (\pi R^2) t$

1st step: Raised to a power $C = A^n$, $\Delta C = C \ln | \frac{\Delta A}{A} |$

$C = R^2 \rightarrow \Delta C = R^2 |2| \frac{\Delta R}{R} = (8.50 \times 10^{-2} \text{ m})^2 |2| \frac{0.02}{8.50}$
 $= (8.50 \times 10^{-2} \text{ m})^2 = 0.34 \times 10^{-4} \text{ m}^2$
 $= 7.23 \times 10^{-3} \text{ m}^2$
 $\Rightarrow (7.23 \times 10^{-3} \pm 0.34 \times 10^{-4}) \text{ m}^2$

2nd step: Multiplication with a scalar $\pi R^2 = 22.7 \times 10^{-3} \pm 1.07$
 $\pi R^2 = (22.7 \times 10^{-3} \pm 1.07 \times 10^{-4}) \text{ m}^2$

3rd step: Multiplication/Division

$C = AB \rightarrow \Delta C = |C| \sqrt{\left(\frac{\Delta A}{A}\right)^2 + \left(\frac{\Delta B}{B}\right)^2}$
 $= (22.7 \times 10^{-3} \text{ m}^2) (0.05 \times 10^{-2} \text{ m})$
 $= 1.14 \times 10^{-5} \text{ m}^3$
 $= |1.14 \times 10^{-5} \text{ m}^3| \sqrt{\left(\frac{1.07 \times 10^{-4}}{22.7 \times 10^{-3}}\right)^2 + \left(\frac{0.005}{0.05}\right)^2}$
 $= 1.14 \times 10^{-6} \text{ m}^3$

$V = (1.1 \pm 0.1) \times 10^{-5} \text{ m}^3$ (2 sig figs)

4. (Motion Along a Straight Line) The position of a particle moving along an x -axis is given by $x = 12t^2 - 2t^3$, where x is in meters and t is in seconds.

- i Determine the acceleration of the particle at $t = 3.0$ s.
- ii What are the maximum positive coordinate reached by the particle and the acceleration of the particle at that instant?

Answer: i) $a(t = 3 \text{ s}) = -12 \text{ m/s}^2$ ii) $x(t = 4 \text{ s}) = 64 \text{ m}$, $a(t = 4 \text{ s}) = -24 \text{ m/s}^2$

i) $x(t) = 12t^2 - 2t^3$
 $v(t) = \frac{dx}{dt} = 24t - 6t^2$ ①
 $a(t) = \frac{dv}{dt} = 24 - 12t \rightarrow a(t=3s) = 24 - 12 \times 3 = -12 \text{ m/s}^2$ ① ①

ii) maximum positive coordinate $\Rightarrow v(t) = \frac{dx}{dt} = 0$ ②
 $24t - 6t^2 = 0 = 6t(4-t) = 0 \Rightarrow t = 4 \text{ s}$ ①
 $\rightarrow x(t=4s) = 12(4)^2 - 2(4)^3 = 192 - 128 = 64 \text{ m}$
 $a(t=4s) = 24 - 12 \times 4 = -24 \text{ m/s}^2$ ① ①

5. (Motion Along a Straight Line) A helicopter is ascending vertically with a speed of 5.40 m/s. At a height of 105 m above the Earth, a package is dropped from the helicopter. How much time does it take for the package to reach the ground? [Hint: What is v_0 for the package?]

Answer: $t = 5.21 \text{ s}$

with our chosen coordinate system
 $v_0 = 5.40 \text{ m/s}$ as upward & $y_i = 0$
 $y_f = -105 \text{ m}$

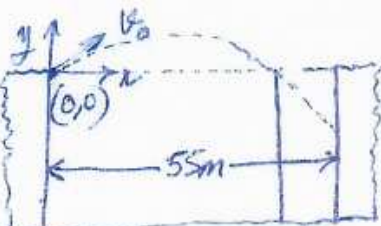
$y - y_0 = v_0 t - \frac{1}{2} g t^2$ (2)
 $-105 - 0 = 5.4t - \frac{1}{2} (9.8)t^2 \Rightarrow 4.9t^2 - 5.4t - 105 = 0$ (2)
 Quadratic equation
 $a t^2 + b t + c = 0$
 $\Rightarrow t_{1,2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-(-5.4) \pm \sqrt{(-5.4)^2 - 4(4.9)(-105)}}{2(4.9)}$
 $= \frac{5.4 \pm \sqrt{29.16 + 2059.8}}{9.8}$
 $\leftarrow \frac{5.21 \text{ s}}{-4.11 \text{ s}} \text{ (2)}$

6. ((Motion in Two and Three Dimensions) A ball is shot from the top of a building with an initial velocity of 18 m/s at an angle $\theta = 42^\circ$ above the horizontal.

i) What are the horizontal and vertical components of the initial velocity?

ii) If a nearby building is the same height and 55 m away, how far below the top of the building will the ball strike the nearby building?

Answer: i) $v_{xo} = 13 \text{ m/s}$ $v_{yo} = 12 \text{ m/s}$ ii) $y = -33 \text{ m}$



$v_0 = 18 \text{ m/s}$
 $\theta = 42^\circ$

i) $v_x = v_0 \cos \theta = 18 \text{ m/s} \cos 42 = 13.38 \text{ m/s}$ (3)
 $v_y = v_0 \sin \theta = 18 \text{ m/s} \sin 42 = 12.04 \text{ m/s}$ (3)

ii) $v_x = v_{0x}$ & $\Delta x = v_{0x} t \rightarrow$ time of flight (3)
 $t = \frac{\Delta x}{v_{0x}} = \frac{55 \text{ m}}{13.38 \text{ m/s}} = 4.11 \text{ s}$ (1)

same time interval for y direction & $y_0 = 0$ (2)

$$\Delta y = y - y_0 = v_{0y} t - \frac{1}{2} g t^2$$

$$= (12.04)(4.11) - \frac{1}{2} (9.8)(4.11)^2$$

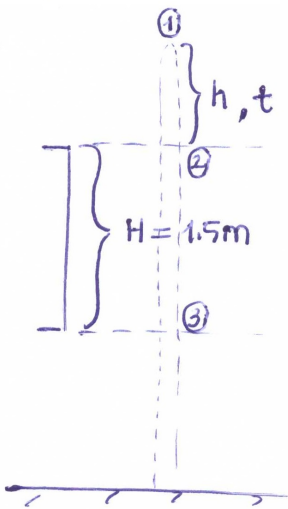
$$= \underline{\underline{-33.3 \text{ m}}}$$
 (2) (1)

{ minus sign shows below the top of the building

7. (Motion Along a Straight Line) A boy sees a flower pot sail up and then back past a window 1.5m high. If the total time the pot is in sight is 1.0s, find the height above the top of the window that the pot rises.

Answer: 1.5 cm

$t =$ time of ascent through a height 'h' = time of descent through a height



Choose downward as the positive y-direction

$$\Delta y = v_{0y} t + \frac{1}{2} a_y t^2$$

$$\text{from 1 to 2: } h = \frac{1}{2} g t^2$$

$$\text{from 1 to 3: } h + H = \frac{1}{2} g \left(t + \frac{1}{2}\right)^2$$

$$\frac{1}{2} g t^2 + H = \frac{1}{2} g t^2 + g \frac{t}{2} + \frac{g}{8}$$

$$1.5 = (9.8) \cdot \frac{t}{2} + \frac{9.8}{8}$$

$$t = 0.056 \text{ s}$$

$$h = \frac{1}{2} (9.8 \text{ m/s}^2) (0.056 \text{ s})^2 = 15 \text{ cm}$$

8. (Vectors) For the following three vectors, what is $3\vec{C} \cdot (2\vec{A} \times \vec{B})$

$$\vec{A} = 2.00\hat{i} + 3.00\hat{j} - 4.00\hat{k},$$

$$\vec{B} = -3.00\hat{i} + 4.00\hat{j} + 2.00\hat{k},$$

$$\vec{C} = 7.00\hat{i} - 8.00\hat{j}$$

Answer: 540

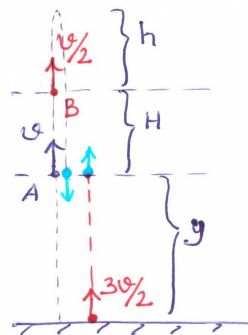
Handwritten solution showing the calculation of the dot product $3\vec{C} \cdot (2\vec{A} \times \vec{B})$. The steps are as follows:

$$2\vec{A} = 4\hat{i} + 6\hat{j} - 8\hat{k} \quad (2)$$
$$3\vec{C} = 21\hat{i} - 24\hat{j} \quad (2)$$
$$2\vec{A} \times \vec{B} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 4 & 6 & -8 \\ -3 & 4 & 2 \end{vmatrix} = (12 + 32)\hat{i} - (8 - 24)\hat{j} + (16 + 18)\hat{k} \quad (1)$$
$$= 44\hat{i} + 16\hat{j} + 34\hat{k} \quad (2)$$
$$3\vec{C} \cdot (2\vec{A} \times \vec{B}) = (21\hat{i} - 24\hat{j}) \cdot (44\hat{i} + 16\hat{j} + 34\hat{k}) \quad (1)$$
$$= 21 \cdot 44 - 24 \cdot 16 = \boxed{540} \quad (2)$$

9. (Motion Along a Straight Line) A stone is thrown vertically upward. On its way up it passes point A with speed v , and point B, 3.00 m higher than A, with speed $\frac{v}{2}$.

- Calculate the speed v and the maximum height reached by the stone above point B. At the instant when the first ball is on its way up at point B, second ball is thrown upward from the ground and with an initial speed of $\frac{3v}{2}$.
- How long after the second ball is thrown does it take if the two balls are to meet at the point A.
- What is the height of the point A above the ground if the two balls are to meet at the point A.

Answer: i) $v = 8.86 \text{ m/s}$ $h = 1.00 \text{ m}$ ii) $t = 1.36 \text{ s}$ iii) $y = 9.00 \text{ m}$



$$i) \quad v_y^2 = v_{0y}^2 \pm 2a_y \Delta y$$

$$\left(\frac{v}{2}\right)^2 = v^2 - 2gH$$

$$v = \sqrt{8gH/3} = \sqrt{8(9.81)(3)/3} = 8.86 \text{ m/s}$$

$$0 = \left(\frac{v}{2}\right)^2 - 2gh$$

$$h = \frac{v^2}{8g} = \frac{8.86^2}{8(9.81)} = 1.00 \text{ m}$$

$$ii) \quad \Delta y = v_{0y} t \pm \frac{1}{2} a_y t^2$$

$$-H = \frac{v}{2} t - \frac{1}{2} g t^2$$

$$4.91 t^2 - \frac{8.86}{2} t - 3 = 0 \quad \rightarrow \quad t = \frac{4.43 \pm \sqrt{4.43^2 + 4(4.91)(3)}}{9.81}$$

$$t = 1.36 \text{ s}$$

$$iii) \quad y = \frac{3v}{2} t - \frac{1}{2} g t^2$$

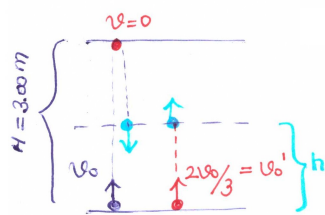
$$= \frac{3}{2} (8.86)(1.36) - \frac{1}{2} (9.81)(1.36)^2$$

$$= 9.00 \text{ m}$$

10. (Motion Along a Straight Line) A juggler performs in a room whose ceiling is 3.00 m above the level of his hands. He throws a ball upward so that it just reaches the ceiling.

- i) What is the initial velocity of the ball?
- ii) What is the time required for the ball to reach the ceiling? At the instant when the first ball is at ceiling, the juggler throws a second ball upward with two-thirds the initial velocity of the first.
- iii) How long after the second ball is thrown did the two balls pass each other?
- iv) At what distance above the juggler's hand do they pass each other?

Answer: i) $v_o = 7.67 \text{ m/s}$ ii) $t = 0.782 \text{ s}$ iii) $t = 0.587 \text{ s}$ iv) $h = 1.31 \text{ m}$



$$i) v_y^2 = v_{oy}^2 \pm 2ay \Delta y$$

$$0 = v_o^2 - 2gH$$

$$v_o = \sqrt{2(9.81)3} = 7.67 \text{ m/s.}$$

$$ii) v_y = v_{oy} \pm ay t$$

$$0 = 7.67 - (9.8)t \rightarrow t = 0.782 \text{ s.}$$

$$iii) \Delta y = v_{oy} t \pm \frac{1}{2} ay t^2$$

$$H - h = 0 + \frac{1}{2} g (t^i)^2 \quad (\text{for the first ball})$$

$$3 - h = \frac{1}{2} (9.81) (t^i)^2$$

$$h = v_o^i t^i - \frac{1}{2} g (t^i)^2$$

$$h = \frac{2}{3} (7.67) t^i - \frac{1}{2} (9.81) (t^i)^2$$

$$3 - 5.11 t^i + 4.91 (t^i)^2 = 4.91 (t^i)^2 \rightarrow t^i = 0.587 \text{ s.}$$

$$h = 1.31 \text{ m}$$

11. (Vectors) Vectors \vec{A} and \vec{B} lie in an xy -plane. \vec{A} has magnitude 8.0 and an angle 130° ; B has components $B_x = -7.72$ and $B_y = -9.20$.

i) What are $5\vec{A} \cdot \vec{B}$ and $4\vec{A} \times 3\vec{B}$ in unit vector notation?

ii) What is $(3\hat{i} + 5\hat{j}) \times (4\vec{A} \times 3\vec{B})$? Find magnitude and angle of resultant vector.

Answer: i) $5\vec{A} \cdot \vec{B} = -83.58$, $4\vec{A} \times 3\vec{B} = 1135.4 \hat{k}$

ii) $|(3\hat{i} + 5\hat{j}) \times (4\vec{A} \times 3\vec{B})| = 6620.5$, $\theta = -31^\circ$ OR $= 329^\circ$

\vec{A} & \vec{B} lie in xy plane \Rightarrow only x & y components
 $|\vec{A}| = 8$ with angle 130° & $B_x = -7.72$, $B_y = -9.20$
 $\Rightarrow \vec{A} = |\vec{A}| \cos 130^\circ \hat{i} + |\vec{A}| \sin 130^\circ \hat{j} = \underline{-5.14 \hat{i} + 6.13 \hat{j}}$
 $\vec{B} = -7.72 \hat{i} + 9.20(-\hat{j}) //$

i) $5\vec{A} \cdot \vec{B} = 5(-5.14 \hat{i} + 6.13 \hat{j}) \cdot (-7.72 \hat{i} - 9.20 \hat{j})$
 $= 5 [(-5.14)(-7.72) + (6.13)(-9.20)] = \underline{-83.58}$

$4\vec{A} \times 3\vec{B} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ -20.56 & 24.52 & 0 \\ -23.16 & -27.6 & 0 \end{vmatrix} = \begin{matrix} (24.52 \times 0 - 0(-27.6)) \hat{i} \\ + (0(-23.16) - (-20.56)0) \hat{j} \\ + ((-20.56)(-27.6) - (24.52)(-23.16)) \hat{k} \end{matrix}$
 $= \underline{1135.4 \hat{k}}$

ii) $(3\hat{i} + 5\hat{j}) \times (1135.4 \hat{k}) = (3 \times 1135.4)(\hat{i} \times \hat{k}) + (5 \times 1135.4)(\hat{j} \times \hat{k})$
 $\hat{i} \rightarrow \hat{j} \rightarrow \hat{k}$
 $= 5677 \hat{i} + 3460.2(-\hat{j})$

Magnitude: $\sqrt{(5677)^2 + (-3460.2)^2} = \underline{6620.5}$
 angle: $\theta = \tan^{-1} \frac{-3460.2}{5677} = \underline{-31^\circ}$ OR $\underline{329^\circ}$

12. (Vectors) Given two vectors, $\vec{A} = 5i - 6.5j$ and $\vec{B} = -3.5i + 7j$. A third vector \vec{C} lies in the xy -plane. Vector \vec{C} is perpendicular to vector \vec{A} , and the scalar product of \vec{C} with \vec{B} is 15.0. From this information, find the components of vector \vec{C} .

Answer: $C_x = 8.0$ and $C_y = 6.1$

$$\begin{aligned} \vec{A} \text{ and } \vec{C} \text{ are perpendicular, so } \vec{A} \cdot \vec{C} &= 0 \\ A_x C_x + A_y C_y &= 0 \\ 5.0 C_x - 6.5 C_y &= 0 \quad (1) \end{aligned}$$

$$\vec{B} \cdot \vec{C} = 15.0, \text{ so } -3.5 C_x + 7.0 C_y = 15.0 \quad (2)$$

We have two equations in two unknowns C_x and C_y .
Solving gives $C_x = 8.0$ and $C_y = 6.1$

13. (Motion in Two and Three Dimensions) The position of an object moving along an x axis is given by $x = 3t - 4t^2 + t^3$, where x is in meters and t is in seconds.

- i What is the object displacement between $t = 3$ s and $t = 4$ s?
- ii What is its average velocity for the time interval $t = 1$ s and $t = 3$ s?
- iii Is there ever a time when the velocity is zero?
- iv What is its instantaneous acceleration at $t = 2$ s?

Answer: i) 12 m ii) 0 m/s iii) 0.45 s, 2.21 s iv) 4 m/s²

i. $\Delta \vec{x} = \vec{x}(t=4s) - \vec{x}(t=3s)$

$x(t=4s) = 3 \cdot 4 - 4 \cdot 4^2 + 4^3 = 12 \text{ m}$

$x(t=3s) = 3 \cdot 3 - 4 \cdot 3^2 + 3^3 = 0 \text{ m}$

$\Delta x = 12 \text{ m} - 0 \text{ m} = 12 \text{ m}$

ii. $v_{\text{Avg}} = \frac{\Delta \vec{x}}{\Delta t} = \frac{\vec{x}(t=3s) - \vec{x}(t=1s)}{3-1}$

$x(t=3s) = 3 \cdot 3 - 4 \cdot 3^2 + 3^3 = 0 \text{ m}$

$x(t=1s) = 3 \cdot 1 - 4 \cdot 1^2 + 1^3 = 0 \text{ m}$

so $v_{\text{avg}} = \frac{0 \text{ m}}{2 \text{ s}} = 0 \text{ m/s}$

iii. $v = \frac{dx}{dt} = 3 - 8t + 3t^2$

$v = 0 \rightarrow 3t^2 - 8t + 3 = 0 \rightarrow t = \frac{8 \pm \sqrt{8^2 - 4(3)(3)}}{6}$

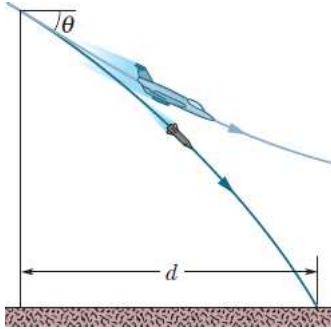
$t_1 = 0.45 \text{ s}$

$t_2 = 2.22 \text{ s}$

iv. $a = \frac{dv}{dt} = -8 + 6t$

$a(t=2s) = -8 + 6 \cdot 2 = 4 \text{ m/s}^2$

14. (Motion in Two and Three Dimensions) A certain airplane has a speed of 290.0 km/h and is diving at an angle of $\theta = 30.0^\circ$ below the horizontal when the pilot releases a radar decoy (see Figure below). The horizontal distance between the release point and the point where the decoy strikes the ground is $d = 700 \text{ m}$.



- i How long is the decoy in the air?
- ii How high was the release point?

Answer: i) 10 s ii) 893 m

$$a) v_0 = 290 \text{ km/h} = \frac{290 (1000) \text{ m}}{(60)(60) \text{ s}} = 80.6 \frac{\text{m}}{\text{s}} \quad (2)$$

$$d = v_{0x} \cdot t \quad (2)$$

$$d = v_0 \cos \theta \cdot t \quad (2)$$

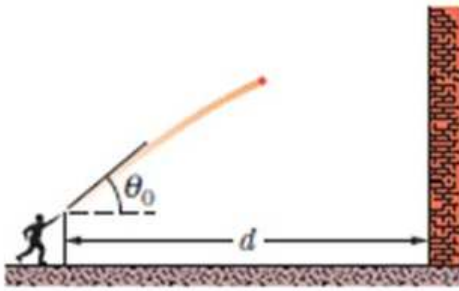
$$700 = (80.6) \cos 30^\circ \cdot t \Rightarrow t = 10 \text{ s} \quad (2) \quad (1) \quad (1)$$

$$b) -h = -v_0 \sin \theta \cdot t - \frac{1}{2} g t^2 \quad (2)$$

$$h = (80.6) \sin 30^\circ (10) + \frac{1}{2} (9.8) (10)^2 \quad (6)$$

$$= 893 \text{ m} \quad (1) \quad (1)$$

15. (Motion in Two and Three Dimensions) You throw a ball toward a wall at speed 25.0 m/s and at angle $\theta_0 = 40.0^\circ$ above the horizontal (as given in figure below). The wall has a distance $d = 22.0 \text{ m}$ from the release point of the ball.



- i How far above the release point does the ball hit the wall?
- ii What are the horizontal and vertical components of its velocity as it hits the wall?
- iii When it hits, has it passed the highest point on its trajectory?

Answer: i) 12 m ii) $v_x = 19.2 \text{ m/s}$, $v_y = 4.8 \text{ m/s}$ iii) NO

i) Horizontal

$$d = v_{0x} t \rightarrow d = v_0 \cos \theta_0 t \rightarrow t = \frac{d}{v_0 \cos \theta_0} = \frac{22 \text{ m}}{(25 \frac{\text{m}}{\text{s}}) \cos 40}$$

$$t = 1.15 \text{ s}$$

Vertical

$$y - y_0 = v_{0y} t - \frac{1}{2} g t^2 \Rightarrow y = v_0 \sin \theta_0 t - \frac{1}{2} g t^2$$

$$y = (25 \text{ m/s}) (\sin 40) (1.15) - (4.9 \frac{\text{m}}{\text{s}^2}) (1.15)^2$$

$$= 12 \text{ m.}$$

ii) $v_x = v_{0x} = v_0 \cos \theta_0 = (25 \text{ m/s}) (\cos 40^\circ) = 19.2 \text{ m/s.}$

$$v_y = v_{0y} - g t = v_0 \sin \theta - g t = (25 \text{ m/s}) \sin 40^\circ - (9.8 \text{ m/s}^2) (1.15)$$

$$= 4.80 \text{ m/s.}$$

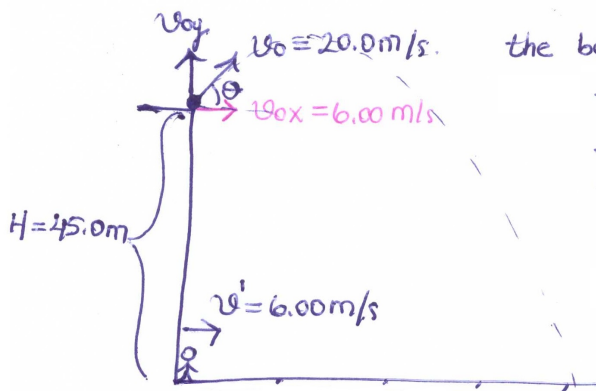
iii) When the ball hits the ground since $v_y = 4.8 \text{ m/s} > 0$ then it hasn't passed the highest point on its trajectory!!

16. (Motion in Two and Three Dimensions) A 2.7 kg ball is thrown upward with an initial speed of 20.0 m/s from the edge of a 45.0 m high cliff. At the instant the ball is thrown, a woman starts running away from the base of the cliff with a constant speed of 6.00 m/s . The woman runs in a straight line on level ground. Ignore air resistance on the ball.

i At what angle above the horizontal should the ball be thrown so that the runner will catch it just before it hits the ground?

ii How far does she run before she catches the ball?

Answer: i) $\theta_0 = 72.5^\circ$ ii) 33.3 m



the ball moves in projectile motion.

The woman and the ball travel for the same time and must travel the same horizontal distance so for the ball $v_{0x} = 6.00 \text{ m/s}$.

$$i. v_{0x} = v_0 \cos \theta$$

$$\theta = \cos^{-1} \left(\frac{v_{0x}}{v_0} \right)$$

$$\theta = \cos^{-1} \left(\frac{6.00 \text{ m/s}}{20.0 \text{ m/s}} \right) = 72.5^\circ$$

ii. Choose upward as the positive y -direction

$$\Delta y = v_{0y} t + \frac{1}{2} a_y t^2$$

$$-H = v_0 \sin \theta t - \frac{1}{2} g t^2$$

$$-(45.0 \text{ m}) = (20.0 \text{ m/s}) \sin(72.5^\circ) t - \frac{1}{2} (9.81 \text{ m/s}^2) t^2$$

$$t = 5.54 \text{ s}$$

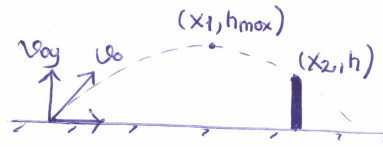
$$\Delta x = v_{0x} t$$

$$\Delta x = (20.0 \text{ m/s}) \cos(72.5^\circ) (5.54 \text{ s}) = 33.3 \text{ m}$$

17. (Motion in Two and Three Dimensions) A ball is hit at ground level. The ball reaches its maximum height above ground level 3.0 s after being hit. Then 2.5 s after reaching its maximum height, the ball barely clears a fence that is 97.5 m from where it was hit.

- i) What maximum height above ground level is reached by the ball?
- ii) How high is the fence?
- iii) How far beyond the fence does the ball strike the ground?

Answer: i) 44.1 m ii) 13.4 m iii) 8.86 m



The trajectory of the baseball is shown in the figure. At $t_1 = 3.0$ s, the ball reaches the maximum height h_{\max} , and at $t_2 = t_1 + 3.0$ s = 5.5 s, it barely clears a fence at $x_2 = 97.5$ m.

Choose downward as the positive y -direction

$$i) \Delta y = v_{0y} t + \frac{1}{2} a_y t^2$$

$$h_{\max} = 0 + \frac{1}{2} g t_1^2$$

$$h_{\max} = \frac{1}{2} (9.8 \text{ m/s}^2) (3.0 \text{ s})^2 = 44.1 \text{ m}$$

$$ii) (h_{\max} - h) = 0 + \frac{1}{2} g (t_2 - t_1)^2$$

$$44.1 \text{ m} - h = \frac{1}{2} (9.8 \text{ m/s}^2) (2.5)^2 \rightarrow h = 13.48 \text{ m} \approx 13 \text{ m}$$

$$iii) x = v_{0x} t$$

$$97.5 \text{ m} = v_{0x} (5.5 \text{ s}) \rightarrow v_{0x} = 17.7 \text{ m/s}$$

The total flight time of the ball is $T = 2t_1 = 2(3.0 \text{ s}) = 6.0 \text{ s}$

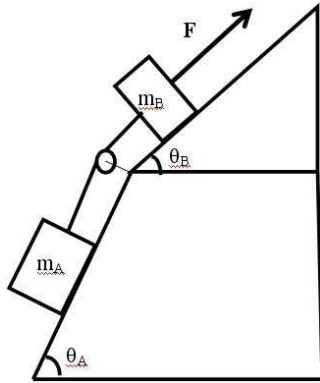
Thus, the range of baseball is

$$R = v_{0x} T = (17.7 \text{ m/s})(6.0 \text{ s}) = 106.4 \text{ m}$$

which means that the ball travels an additional distance

$$\Delta x = R - x_2 = 106.4 \text{ m} - 97.5 \text{ m} = 8.86 \text{ m} \approx 8.9 \text{ m}$$

18. (Force and Motion - I) Consider the system shown in figure with $m_A = 9.5 \text{ kg}$ and $m_B = 11.5 \text{ kg}$. The angles $\theta_A = 59^\circ$ and $\theta_B = 32^\circ$.



- Draw the free body diagrams for block A and block B.
- In the absence of friction, what force F would be required to pull the masses at a constant velocity up?
- The force F now is removed. What is the magnitude and direction of acceleration of the two blocks?
- In the absence of F , what is the tension in the string?

Answer: ii) 140 N iii) $\vec{a} = -6.7 \text{ m/s}^2 \hat{i}$ iv) 17 N

Handwritten solution for the physics problem:

i) Free Body Diagrams (FBDs) for mass A and mass B. For mass A, forces shown are tension T up the incline, normal force F_N perpendicular to the incline, and weight $m_A g$ vertically down. For mass B, forces shown are tension T up the incline, normal force F_N perpendicular to the incline, weight $m_B g$ vertically down, and an external force F up the incline.

ii) Constant velocity ($a = 0$):

Mass A: $T - m_A g \sin \theta_A = 0$
 Mass B: $F - T - m_B g \sin \theta_B = 0$

Adding equations: $F = T + m_B g \sin \theta_B = m_A g \sin \theta_A + m_B g \sin \theta_B$
 $= (9.5 \sin 59^\circ + 11.5 \sin 32^\circ) 9.8 = 7.93 \text{ N} + 5.97 \text{ N} \approx 140 \text{ N}$

iii) Now $a \neq 0$:

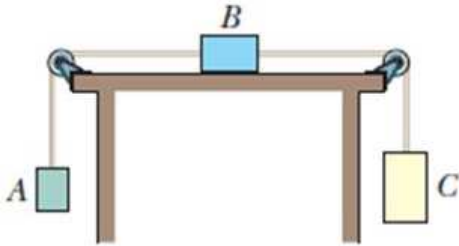
Mass A: $T - m_A g \sin \theta_A = m_A a$
 Mass B: $F - T - m_B g \sin \theta_B = m_B a$

Adding equations: $F = m_A (g \sin \theta_A + a) + m_B (g \sin \theta_B + a)$
 $\Rightarrow a = \frac{F - m_A g \sin \theta_A - m_B g \sin \theta_B}{m_A + m_B} = \frac{140 - 79.3 - 59.7}{9.5 + 11.5} = \frac{-6.7}{21} \approx -6.7 \text{ m/s}^2$

iv) Tension T when $F = 0$ and $a = -6.7 \text{ m/s}^2$:

Mass A: $T - m_A g \sin \theta_A = m_A a$
 $T = m_A (a + g \sin \theta_A) = 9.5 (-6.7 + 9.8 \sin 59^\circ) \approx 16.2 \text{ N}$

19. (Force and Motion - I) Figure shows three blocks attached by cords that loop over **frictionless** table. The masses are $m_A = 6 \text{ kg}$, $m_B = 8 \text{ kg}$ and $m_C = 10 \text{ kg}$.



- What is the acceleration of the system?
- When the blocks are released, what is the tension in the cord at the right?
- When the blocks are released, what is the tension in the cord at the left?

Answer: i) $a = 1.63 \text{ m/s}^2$ ii) $T_C = 81.67 \text{ N}$ iii) $T_A = 68.6 \text{ N}$

Free-body diagrams for blocks A, B, and C are shown at the top. Block A has forces T_A (up) and $m_A g$ (down). Block B has forces T_A (left) and T_C (right). Block C has forces T_C (up) and $m_C g$ (down).

i) $T_A - m_A g = m_A a$ (1) & $T_C - T_A = m_B a$ (2) & $m_C g - T_C = m_C a$ (3)

① ② ③ into ② $m_C(g-a) - m_A(a+g) = m_B a$

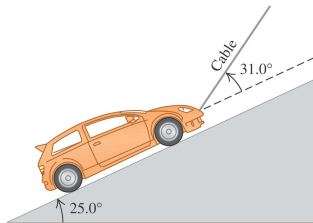
$(m_C - m_A)g = a(m_B + m_C + m_A)$

$\Rightarrow a = \frac{(10\text{kg} - 6\text{kg}) \cdot 9.8 \text{ m/s}^2}{(8\text{kg} + 8\text{kg} + 10\text{kg})} = \frac{1}{6} \cdot 9.8 \text{ m/s}^2 = 1.63 \text{ m/s}^2$

ii) $T_C = m_C(g-a) = 10\text{kg} \left(\frac{5}{6}g\right) = 10\text{kg} \left(\frac{5}{6}\right) 9.8 \text{ m/s}^2 = 81.67 \text{ N}$

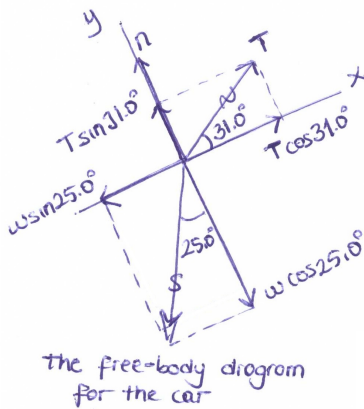
iii) $T_A = m_A(g+a) = 6\text{kg} \left(\frac{7}{6}g\right) = 6\text{kg} \left(\frac{7}{6}\right) 9.8 \text{ m/s}^2 = 68.6 \text{ N}$

20. (Force and Motion - I) A 1130 kg car is held in place by a light cable on a frictionless ramp shown in the figure. The cable makes an angle of 31.0° above the surface of the ramp, and the ramp itself rises at 25.0° above the horizontal.



- i Draw a free-body diagram for the car.
- ii Find the tension in the cable.
- iii How hard does the surface of the ramp push on the car?

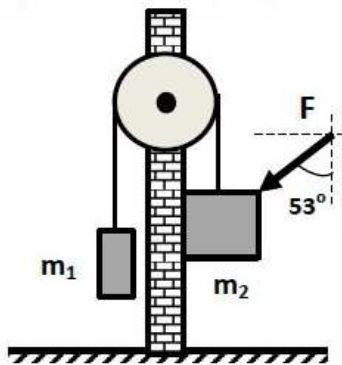
Answer: ii) 5460 N iii) 7220 N



$$\begin{aligned}
 \text{i) } \sum F_x &= 0 \\
 T \cos 31.0^\circ - w \sin 25.0^\circ &= 0 \\
 T &= w \frac{\sin 25.0^\circ}{\cos 31.0^\circ} \\
 T &= (1130 \text{ kg})(9.80 \text{ m/s}^2) \frac{\sin 25.0^\circ}{\cos 31.0^\circ} \\
 T &= 5460 \text{ N}
 \end{aligned}$$

$$\begin{aligned}
 \text{ii) } \sum F_y &= 0 \\
 n + T \sin 31.0^\circ - w \cos 25.0^\circ &= 0 \\
 n &= w \cos 25.0^\circ - T \sin 31.0^\circ \\
 n &= (1130 \text{ kg})(9.80 \text{ m/s}^2) - (5460 \text{ N}) \sin 31.0^\circ = 7220 \text{ N}
 \end{aligned}$$

21. (Force and Motion - II) Two blocks of masses $m_1 = 1 \text{ kg}$ and $m_2 = 2 \text{ kg}$ are suspended by a cord from a pulley which is attached to in front of a wall as shown in figure. A horizontal force of 8.3 N is applied to second block and the coefficients of static and kinetic frictions between the wall and the second block are 0.4 and 0.2 . Cord and pulley are massless and pulley is frictionless.



If the blocks, which are initially at rest, start moving when they are released;

- i Draw the free body diagrams for both blocks.
- ii Find the acceleration of the blocks.

Answer: ii) $a = 4.49 \text{ m/s}^2$

i) FBDs

ii) Equations of motion. Newton's 2nd Law

m_1 : y $T - m_1g = m_1a \rightarrow T = m_1(g+ a)$ (2)

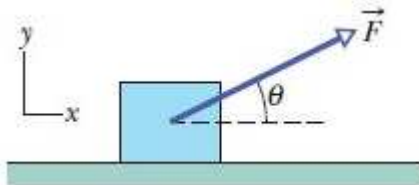
m_2 : x $F_N - F \sin 53^\circ = m_2 a_x = 0 \rightarrow F_N = F \sin 53^\circ$ (2) $f_k = \mu_k F_N$ (1)

y $m_2g + F \cos 53^\circ - f_k - T = m_2a \Rightarrow m_2g + F \cos 53^\circ - \mu_k F \sin 53^\circ - m_1(g+ a) = m_2a$ (3)

$\Rightarrow \frac{(m_2 - m_1)g + F(\cos 53^\circ - \mu_k \sin 53^\circ)}{(m_1 + m_2)} = a$ (2)

$a = \frac{(2 \text{ kg} - 1 \text{ kg}) 9.8 \text{ m/s}^2 + 8.3 \text{ N} (\cos 53^\circ - 0.2 \sin 53^\circ)}{3 \text{ kg}} = 4.49 \text{ m/s}^2$ (1)

22. (Force and Motion - II) Figure shows an initially stationary block of mass m on a floor. A force of magnitude $0.500mg$ (where m is the mass and g is the gravitational acceleration) is then applied at upward angle $\theta = 20^\circ$.



What is the magnitude of the acceleration of the block across the floor if the friction coefficients are

i $\mu_s = 0.600$ and $\mu_k = 0.500$

ii $\mu_s = 0.400$ and $\mu_k = 0.300$?

Answer: i) $a=0$ since no motion ii) 2.17 m/s^2

$\mu_s = 0.400$ and $\mu_k = 0.300$

Equations of motion

x: $F \cos 20 - f_k = ma_x$ (1)

y: $F \sin 20 + F_N - mg = ma_y = 0$ (2)

from (2) $F_N = mg - F \sin 20$ & $f_k = \mu_k F_N$

\Rightarrow (1) $F \cos 20 - \mu_k (mg - F \sin 20) = ma$

$\Rightarrow a = \frac{F}{m} (\cos 20 + \mu_k \sin 20) - \mu_k g$

i) $\mu_s = 0.600$ & $\mu_k = 0.500$ } $\sin 20 = 0.342$ & $\cos 20 = 0.940$

$f_{s, \max} = \mu_s F_N = \mu_s (mg - F \sin 20) = 0.600 (mg - 0.500mg \sin 20) = 0.497mg$ (1)

$F \cos 20 - f_{s, \max} = ma$ } $0.500mg \cdot 0.940 - 0.497mg = ma$ (2)

(1) $(0.470 - 0.497)mg = ma$

negative \rightarrow no motion $a=0$ (2)

ii) $\mu_s = 0.400$ & $\mu_k = 0.300$ (2)

$f_{s, \max} = 0.400 (mg - 0.500mg \sin 20) = 0.332mg$

(1) $(0.470 - 0.332)mg = ma \rightarrow$ positive \Rightarrow motion (2)

if motion exists, we use μ_k

$F \cos 20 - f_k = ma$ } $F \cos 20 - \mu_k (mg - F \sin 20) = ma$ (2)

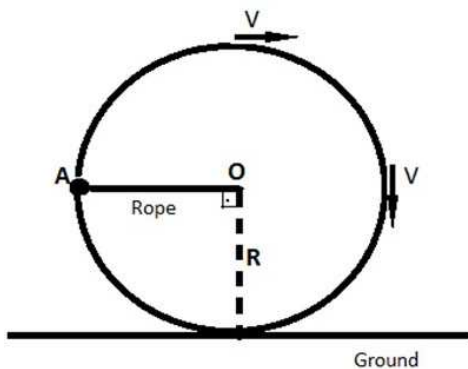
$0.500mg \cdot 0.940 - 0.300 (mg - 0.500mg \cdot 0.342) = ma$

$mg (0.500 \cdot 0.940 - 0.300 + 0.300 \cdot 0.500 \cdot 0.342) = ma$

$\Rightarrow a = 0.221 \times (9.8 \text{ m/s}^2)$

$a = 2.17 \text{ m/s}^2$ (1)

23. (Force and Motion - II) A stone which tied to a rope is rotated in a circular path with a constant speed V in clockwise direction as given in figure below. At point A , the rope is breaking up and the stone is released. The radius R of the circular path is 0.50 m .



If the period of the motion is given as $T = \pi/20\text{ s}$ calculate;

- Magnitude of the centripetal acceleration, a .
- Time required that the stone hit the ground, t .
- Maximum height of the stone with respect to ground, y_{max} .

Hint: Choose the point A as your origin of the your reference frame.

Answer: i) 800 m/s^2 ii) 4.11 s iii) 20.91 m

i) $v = \frac{2\pi R}{T} = \frac{2\pi (0.5\text{m})}{(\frac{\pi}{20}\text{s})} = 20\text{m/s}$ (2)
 $a = \frac{v^2}{R} = \frac{(20\text{m/s})^2}{(0.5\text{m})} = 800\text{m/s}^2$ (3)

ii) $y_{max} = h + R$ (1)
 $h = \frac{v_{oy}^2 - v_y^2}{2g}$ where $v_{oy} = v$
 $v_y = 0$ (at max height)
 $h = \frac{(20\text{m/s})^2}{2(9.8\text{m/s}^2)}$ (2)
 $h = 20.41\text{m}$ (2)
 $y_{max} = h + R = 20.41\text{m} + 0.5\text{m}$
 $y_{max} = 20.91\text{m}$ (2)

iii) $y - y_0 = v_{oy}t - \frac{1}{2}gt^2$
 $-R = v_y t - \frac{1}{2}gt^2$ (1)
 $-0.5 = 20t - 4.9t^2$
 $4.9t^2 - 20t - 0.5 = 0$ (2)
 $t_{1,2} = \frac{-20 \pm \sqrt{400.8}}{2(4.9)}$ (2)
 $t = 4.11\text{s}$ take positive root.

ii) you can find the time required to reach from point A to point B t_{AB} , then find the time required to reach from point B to point A, t_{BA}

then $t = t_{AB} + t_{BA}$
 $t = 2.06\text{s} + 2.07\text{s}$
 $t = 4.11\text{s}$

24. (Force and Motion - II) An astronaut is rotated in a horizontal centrifuge at a radius of 5.0 m.

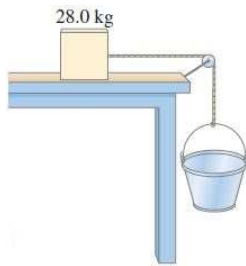
- i) What is the astronaut's speed if the centripetal acceleration has a magnitude of $6.0g$? (g is the gravitational acceleration)
- ii) How many revolutions per minute are required to produce this acceleration?
- iii) What is the period of the motion?

Answer: i) 17.15 m/s ii) 32.7 rev iii) 1.83 s

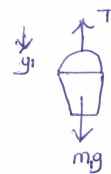
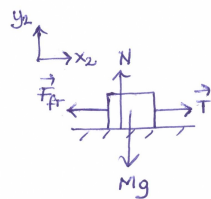
The image shows handwritten calculations for the three parts of the problem. Part (i) uses the centripetal acceleration formula $a = \frac{v^2}{r}$ to solve for v , resulting in $v = 17.15 \text{ m/s}$. Part (ii) uses the period formula $T = \frac{2\pi r}{v}$ to find $T = 1.83 \text{ s}$. Part (iii) uses the frequency formula $n = \frac{t}{T}$ to find $n = 32.7$ revolutions per minute. Red circles with numbers 1, 2, and 3 are placed around the variables and final answers in each step.

$$\text{i)} \quad a = \frac{v^2}{r} \Rightarrow v = \sqrt{a_1 r} = \sqrt{6g \cdot r} = \sqrt{6 \cdot (9.8 \text{ m/s}^2) \cdot 5 \text{ m}} \\ \boxed{v = 17.15 \text{ m/s}}$$
$$\text{ii)} \quad T = \frac{2\pi r}{v} = \frac{2\pi(5 \text{ m})}{17.15 \text{ m/s}} = \boxed{1.83 \text{ s}}$$
$$\text{iii)} \quad n = \frac{t}{T} = \frac{1 \text{ min}}{1.83 \text{ s}} = \frac{60 \text{ s}}{1.83 \text{ s}} = \boxed{32.7}$$

25. (Force and Motion - II) A 28.0 kg block is connected to an empty 2.00 kg bucket by a cord running over a frictionless pulley as shown in the figure. The coefficient of static friction between the table and the block is 0.45 and the coefficient of kinetic friction between the table and the block is 0.32. Sand is gradually added to the bucket until the system just begins to move. **Answer: i) 10.6 kg ii) 0.88 m/s²**



- i Calculate the mass of sand added to the bucket.
ii Calculate the acceleration of the system.



Consider the free-body diagrams for both objects, initially stationary. As sand is added, the tension will increase, and the force of static friction on the block will increase until it reaches

its maximum of $F_{fr} = \mu_s N$. Then the system will start to move.

i) When the static frictional force is at its maximum, but the objects are still stationary;

$$\text{for the bucket: } \Sigma F_y = 0 \rightarrow m_1 g - T = 0 \rightarrow T = m_1 g$$

$$\text{for the block: } \Sigma F_y = 0 \rightarrow N - Mg = 0 \rightarrow N = Mg$$

$$\Sigma F_x = 0 \rightarrow T - F_{fr} = 0 \rightarrow T = F_{fr}, F_{fr} = \mu_s N$$

$$m_1 g = \mu_s M g$$

$$m_1 = (0.45)(28.0 \text{ kg})$$

$$m_1 = 12.6 \text{ kg}$$

Thus 12.6 kg - 2.00 kg = 10.6 kg \approx 11 kg of sand was added.

ii) Now the objects will accelerate. $a_{y1} = a_{x2} = a$. The frictional force is now kinetic friction, given by $F_{fr} = \mu_k N = \mu_k M g$

$$\text{for the bucket: } \Sigma F_y = m_1 a \rightarrow m_1 g - T = m_1 a \rightarrow T = m_1 g - m_1 a$$

$$\text{for the block: } \Sigma F_x = M a \rightarrow T - F_{fr} = M a \rightarrow T = F_{fr} + M a$$

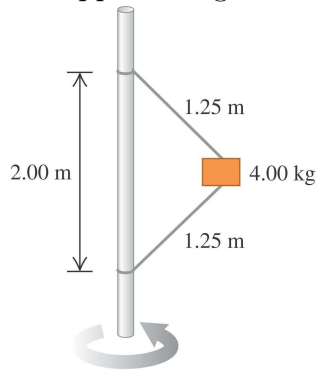
$$m_1 g - m_1 a = F_{fr} + M a$$

$$(12.6 \text{ kg})(9.80 \text{ m/s}^2) - (12.6 \text{ kg}) a = (0.32)(28.0 \text{ kg})(9.80 \text{ m/s}^2)$$

$$(12.6 \text{ kg})(9.80 \text{ m/s}^2) - (12.6 \text{ kg}) a = (0.32)(28.0 \text{ kg})(9.80 \text{ m/s}^2) + (28.0 \text{ kg}) a$$

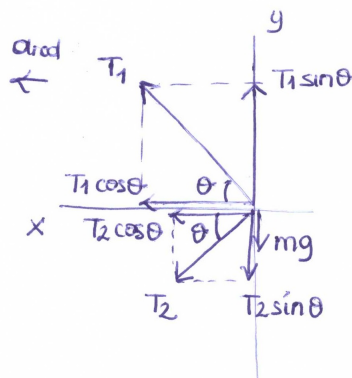
$$a = 0.88 \text{ m/s}^2$$

26. (Force and Motion - II) A 4.00 kg block is attached to a vertical rod by means of two strings. When the system rotates about the axis of the rod, the strings are extended as shown in the figure and the tension in the upper string is 80.0 N .



- i) What is the tension in the lower cord?
 ii) How many revolutions per minute does the system make?

Answer: i) 31.0 N ii) 44.9 rev/min



$$\sin \theta = \frac{1.00 \text{ m}}{1.25 \text{ m}} \rightarrow \theta = 53.1^\circ$$

$$\text{i) } \sum F_y = 0$$

$$T_1 \sin \theta - T_2 \sin \theta - mg = 0$$

$$(80.0 \text{ N}) \sin 53.1^\circ - T_2 \sin 53.1^\circ - (4.00 \text{ kg})(9.81 \text{ m/s}^2)$$

$$T_2 = 31.0 \text{ N}$$

$$\text{ii) } \sum F_x = \text{max}$$

$$T_1 \cos \theta + T_2 \cos \theta = m \frac{v^2}{r}, \quad r = (1.25 \text{ m}) \cos 53.1^\circ = 0.75 \text{ m}$$

$$(80.0 \text{ N}) \cos 53.1^\circ + (31.0 \text{ N}) \cos 53.1^\circ = (4.00 \text{ kg}) \frac{v^2}{0.75 \text{ m}}$$

$$v = 3.53 \text{ m/s}$$

$$f = \frac{v}{2\pi r} = \frac{3.53 \text{ m/s}}{2\pi (0.75 \text{ m})} = 0.749 \frac{\text{rev}}{\text{s}} \cdot \frac{60 \text{ s}}{1 \text{ min}} = 44.9 \text{ rev/min}$$



İzmir Kâtip Çelebi University
Department of Engineering Sciences
Phy101 Physics I
Midterm Examination
April 07, 2019 10:30 – 12:30
Good Luck!

NAME-SURNAME:

SIGNATURE:

ID:

DEPARTMENT:

DURATION: 120 minutes

- ◇ Answer all the questions.
- ◇ Write the solutions explicitly and clearly.
Use the physical terminology.
- ◇ You are allowed to use Formulae Sheet.
- ◇ Calculator is allowed.
- ◇ You are not allowed to use any other electronic equipment in the exam.

Question	Grade	Out of
1A		15
1B		15
2		20
3		20
4		20
5		20
TOTAL		110

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1. A) Estimate the number of breaths taken during an average life time.
 (Hints: YOU estimate; the typical life time, the average number of breaths that a person takes in 1 min. Use chain rule. Use scientific notation in your final result.)

Typical life span is 70 years.

2 pt (estimation) ← 10 breathes per minute is the average number for all situations which contain exercising, angry, sleeping, serene & so forth.

The # of minutes per year: $1 \text{ yr} \times 400 \frac{\text{days}}{\text{yr}} \times \frac{25 \text{ h}}{\text{day}} \times 60 \frac{\text{min}}{\text{h}} = 6 \times 10^5 \frac{\text{min}}{\text{yr}}$ conversion by chain: 10 pt

(To multiply 400×25 is simpler than 365×24 !)

$(70 \text{ yr})(6 \times 10^5 \text{ min/yr}) = 4 \times 10^7 \text{ min}$

At a rate of 10 breathes/min, an individual would take $\frac{4 \times 10^8}{10}$ breathes in a lifetime.

3 pt

- B) The radius of a solid sphere is measured to be (13.00 ± 0.40) cm, and its mass is measured to be (3.70 ± 0.04) kg. Determine the density of the sphere in kilograms per cubic meter and the uncertainty in the density.

$$\begin{aligned}
 & R = (6.50 \pm 0.20) \text{ cm} = (6.50 \pm 0.20) \times 10^{-2} \text{ m} \\
 & m = (1.85 \pm 0.02) \text{ kg} \quad \text{(3 sig figs)} \quad \left. \begin{array}{l} \rho = \frac{m}{V} = \frac{m}{\frac{4\pi R^3}{3}} \\ \text{Three steps} \end{array} \right\}
 \end{aligned}$$

1st step: Raised to a power $C = A^n \rightarrow \Delta C = C \ln | \frac{\Delta A}{A} |$ (2)

$$\begin{aligned}
 C = R^3 & \rightarrow \Delta C = R^3 / 3 | \frac{\Delta R}{R} = (2.75 \times 10^{-4} \text{ m}^3) / 3 | \frac{0.20 \times 10^{-2} \text{ m}}{6.50 \times 10^{-2} \text{ m}} \\
 & = (6.50 \times 10^{-2} \text{ m})^3 = 2.75 \times 10^{-4} \text{ m}^3 \\
 & = 2.54 \times 10^{-5} \text{ m}^3 \\
 & \Rightarrow (2.75 \times 10^{-4} \pm 2.54 \times 10^{-5}) \text{ m}^3 \quad (2)
 \end{aligned}$$

2nd step: Multiplication with a scalar (2)

$$\frac{4\pi}{3} (2.75 \times 10^{-4} \pm 2.54 \times 10^{-5}) \text{ m}^3 = (1.15 \times 10^{-3} \pm 1.06 \times 10^{-4}) \text{ m}^3$$

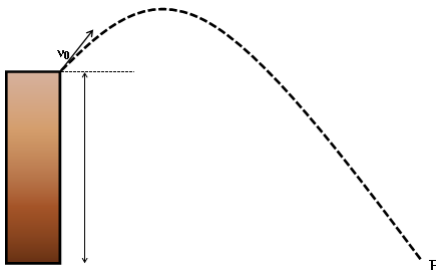
3rd step: Multiplication/Division $C = \frac{A}{B} \rightarrow \Delta C = |C| \sqrt{(\frac{\Delta A}{A})^2 + (\frac{\Delta B}{B})^2}$ (2)

$$\begin{aligned}
 \frac{(1.85 \pm 0.02) \text{ kg}}{(1.15 \times 10^{-3} \pm 1.06 \times 10^{-4}) \text{ m}^3} & \Rightarrow C = \frac{1.85 \text{ kg}}{1.15 \times 10^{-3} \text{ m}^3} \rightarrow \Delta C = |1.61 \times 10^3 \text{ kg/m}^3| \sqrt{(\frac{0.02}{1.85})^2 + (\frac{1.06 \times 10^{-4}}{1.15 \times 10^{-3}})^2} \\
 & = 1.61 \times 10^3 \text{ kg/m}^3 = 0.149 \times 10^3 \text{ kg/m}^3 \quad (3) \\
 & \Rightarrow \boxed{(1.61 \pm 0.15) \times 10^3 \text{ kg/m}^3} \rightarrow (1.6 \pm 0.2) \times 10^3 \text{ kg/m}^3 \quad (1) \quad (2)
 \end{aligned}$$

2. A physics book is dropped from a bridge, falling 90 m to the valley below the bridge.
- In how much time does it pass through the last 20% of its fall?
 - What is its speed when it begins that last 20% of its fall?
 - What is its speed when it reaches the valley beneath the bridge?

$y - y_0 = -\frac{1}{2}gt^2$ (3) } Thus the time for full fall
 $y - y_0 = -90\text{ m}$ (2) } is found to be $t = 4.29\text{ s}$.
 ↓ (2)
 because upward is chosen as
 (+) y direction!
 The first 80% of its free-fall distance is given
 by $-\frac{1}{2}g\tau^2 = -\frac{1}{2}g\tau^2$, which requires $\tau = 3.83\text{ s}$. (2)
 a) Thus, the final 20% of its fall takes
 $t - \tau = 0.45\text{ s}$ (3)
 b) the speed $v = -g\tau$. (3)
 $|v| = 38\text{ m/s}$ approximately. (2)
 c) Similarly, $v_{\text{final}} = -gt \Rightarrow |v_{\text{final}}| = 42\text{ m/s}$ (3) (2)

3. A projectile is shot from the edge cliff 120 m above ground level with an initial speed of 60 m/s at an angle of 30° with the horizontal.



- Determine the distance X of point P from the base of the vertical cliff.
- What is the velocity v at point P in magnitude-angle notation and in unit-vector notation?
- Find the maximum height reached by projectile **above ground**.

$v_0 = 60 \text{ m/s}$
 $\theta = 30^\circ$
 $h_0 = 120 \text{ m}$

$v_{0x} = v_0 \cos \theta$
 $v_{0y} = v_0 \sin \theta$
 $\sin 30^\circ = 0.5$
 $\cos 30^\circ = 0.87$

i) $x = x_0 + v_{0x}t$
 $y = y_0 + v_{0y}t - \frac{1}{2}gt^2$
 $\Rightarrow x - x_0 = v_0 \cos \theta t$
 $X = (60 \text{ m/s}) \cos 30^\circ (8.88 \text{ s})$
 $\approx 461 \text{ m}$

$y - y_0 = v_{0y}t - \frac{1}{2}gt^2$
 $-120 \text{ m} = (60 \text{ m/s}) \sin 30^\circ t - \frac{1}{2} (9.8 \text{ m/s}^2) t^2$
 $\Rightarrow 4.9t^2 - 30t - 120 = 0$
 $t_{1,2} = \frac{-(-30) \pm \sqrt{(-30)^2 - 4(4.9)(-120)}}{2(4.9)}$
 $t_1 = -2.76 \text{ s} \rightarrow \text{not physical} \leftarrow \text{minus sign}$
 $t_2 = 8.88 \text{ s} = t$

ii) At point P
 $v_x = v_{0x} = v_0 \cos \theta$
 $v_y = v_{0y} - gt = v_0 \sin \theta - gt$
 $v_x = (60 \text{ m/s}) \cos 30^\circ$
 $v_y = (60 \text{ m/s}) \sin 30^\circ - (9.8 \text{ m/s}^2)(8.88 \text{ s})$
 $v_x \approx 52 \text{ m/s}$ & $v_y = -57 \text{ m/s}$
 $\vec{v} = v_x \hat{i} + v_y \hat{j} = (52 \hat{i} - 57 \hat{j}) \text{ m/s}$

$|\vec{v}| = \sqrt{(52 \text{ m/s})^2 + (-57 \text{ m/s})^2}$
 $\approx 77.16 \text{ m/s}$
 $\theta = \tan^{-1} \frac{-57}{52} \approx -48^\circ$

iii) $h_{\text{max}} = h_0 + h \rightarrow \text{What is } h?$
 $v_y = v_{0y} - gt = 0$ at max height
 $t_s = \frac{v_{0y}}{g} \rightarrow h = \frac{v_{0y}}{g} v_{0y} - \frac{1}{2}g \left(\frac{v_{0y}}{g}\right)^2$
 $h = \frac{1}{2} \frac{v_0^2 \sin^2 \theta}{g} = \frac{1}{2} \frac{(60 \text{ m/s})^2 \sin^2 30^\circ}{9.8 \text{ m/s}^2}$
 $h \approx 46 \text{ m} \Rightarrow h_{\text{max}} = 120 \text{ m} + 46 \text{ m} = 166 \text{ m}$

4. A boy whirls a stone in a horizontal circle of radius 1.5 m and at height 2.0 m above level ground. The string breaks, and the stone flies off horizontally and strikes the ground after traveling a horizontal distance of 10 m. What is the magnitude of the centripetal acceleration of the stone during the circular motion?

Top view motion

string breaks → Now becomes a projectile motion

$R = 1.5 \text{ m}$

$a_r = \frac{v^2}{R}$, $v = v_0 = ?$ (3)

$x - x_0 = v_0 t$ (2)

$y - y_0 = -\frac{1}{2} g t^2$ (2)

$10 \text{ m} = v_0 t$ (2)

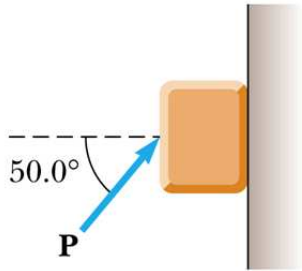
$-2 \text{ m} = -\frac{1}{2} (9.8 \text{ m/s}^2) t^2$ (2)

$t = \sqrt{\frac{2h}{g}} = \sqrt{\frac{2 \times 2 \text{ m}}{9.8 \text{ m/s}^2}} = 0.64 \text{ s}$ (2) (1)

$\Rightarrow v_0 = \frac{10 \text{ m}}{0.64 \text{ s}} = 15.65 \text{ m/s}$ (2) (1)

$a_r = \frac{(15.65 \text{ m/s})^2}{1.5 \text{ m}} = 163.3 \text{ m/s}^2$ (2) (1)

5. A block of mass 3.00 kg is pushed up against a wall by a force P that makes a 50.0° angle with the horizontal as shown in Figure below. The coefficient of static friction between the block and the wall is 0.250.



Determine minimum and maximum values for the magnitude of P that allow the block to remain stationary.

Case 1: Impending upward motion

$$\sum F_x = P \cos 50 - n = 0 \quad (2) \quad \vec{n} \leftarrow$$

$$f_{s, \max} = \mu_s P \cos 50 = 0.161 P$$

$$\sum F_y = 0: P \sin 50 - 0.161 P - 3(9.8) = 0$$

$$P_{\max} = 48.6 \text{ N} \quad (4)$$

Case 2: Impending downward motion

$$\sum F_y = P \sin 50 + 0.161 P - 3(9.8) = 0 \quad (4)$$

$$P_{\min} = 31.7 \text{ N}$$

The handwritten notes include two free-body diagrams. The first diagram, for Case 1, shows a block with forces: $P \sin 50$ (up), $P \cos 50$ (right), n (left), and mg (down). The second diagram, for Case 2, shows a block with forces: $f_{s, \max}$ (up), $P \cos 50$ (right), mg (down), and $P \sin 50$ (up). The normal force n is also shown pointing left in Case 2.