



İzmir Kâtip Çelebi University
Department of Engineering Sciences
Phy102 Physics II
Final Examination
January 09, 2020 13:30 – 15:30
Good Luck!

NAME-SURNAME:

SIGNATURE:

ID:

DEPARTMENT:

INSTRUCTOR:

DURATION: 120 minutes


- ◇ Answer all the questions.
- ◇ Write the solutions explicitly and clearly.
Use the physical terminology.
- ◇ You are allowed to use Formulae Sheet.
- ◇ Calculator is allowed.
- ◇ You are not allowed to use any other electronic equipment in the exam.
- ◇ I declare hereby that I fulfilled the requirements for the attendance according to the University regulations and I accept that my examination will not be valid otherwise.

Question	Grade	Out of
1A		15
1B		15
2		20
3		20
4		20
5		20
TOTAL		110

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1. A) The magnitude J of the current density in a certain lab wire with a circular cross section of radius $R=15.00$ mm is given by $J = (6.00 \times 10^7)r^2$, with J in amperes per square meter and radial distance r in meters. What is the current through the outer section bounded by $r=0.200R$ and $r=0.600R$?

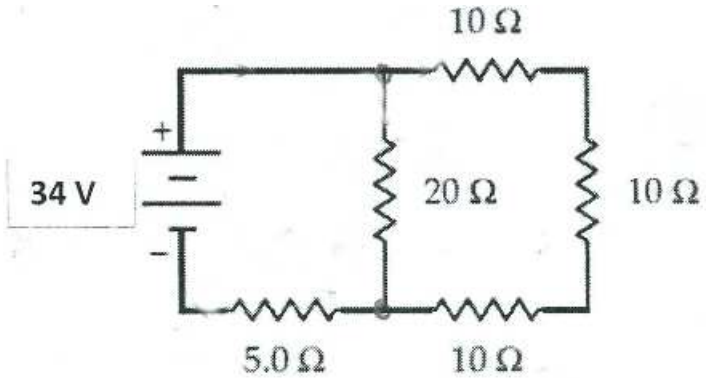
$R = 15 \times 10^{-3} \text{ m}$
 $J(r) = 6 \times 10^7 r^2 \text{ A/m}^2$
 $i = ?$ from $r = 0.2R$
 to $r = 0.6R$



$$\begin{aligned}
 i &= \int \vec{J} \cdot d\vec{A} = \int_{0.2R}^{0.6R} 6 \times 10^7 r^2 2\pi r dr \\
 &= 12\pi \times 10^7 \int_{0.2R}^{0.6R} r^3 dr = 12\pi \times 10^7 \frac{r^4}{4} \Big|_{0.2R}^{0.6R} \\
 &= 3\pi \times 10^7 [(0.6R)^4 - (0.2R)^4] \\
 &= 3\pi \times 10^7 \times 0.128 R^4 = \underline{0.61 \text{ A}}
 \end{aligned}$$

B) For the circuit shown find

- i) the current delivered by the battery,
- ii) the potential difference across the $20\ \Omega$ resistor.



Handwritten solution for problem B:

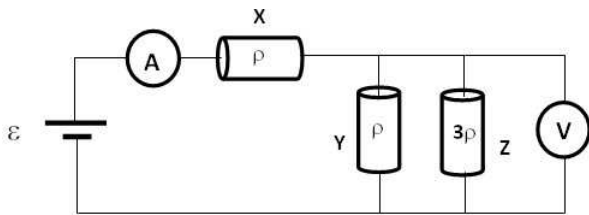
Step 1: Simplify the parallel resistors. $\frac{1}{R_{eq}} = \frac{1}{20\Omega} + \frac{1}{30\Omega}$
 $R_{eq} = \frac{(30\Omega)(20\Omega)}{20\Omega + 30\Omega} = 12\Omega$ (5)

Step 2: Find the current from the battery. $I = \frac{34V}{17\Omega} = 2A$ (5)

Step 3: Find the potential difference across the 20Ω resistor. $V = IR = 12\Omega \times 2A = 24V$ (5)

Step 4: Currents in the parallel branches:
 $I_{20\Omega} = \frac{24V}{20\Omega} = 1.2A$
 $I_{30\Omega} = \frac{24V}{30\Omega} = 0.8A$
 $I = I_1 + I_2$

2. The circuit containing three cylindrical resistors, namely X, Y and Z, which obey Ohm's Law is shown in the figure below. The resistors which have length of L and cross-sectional area of A are connected to an ideal battery of emf ε . As shown an ammeter is connected in series while voltmeter is connected to ends of resistor Z. The resistors X and Y have a resistivity ρ and the resistor Z has a resistivity 3ρ .



i) Find the current i through the ammeter.

ii) Find the reading of voltmeter. (Hint: Multi-loop circuit. Apply junction and loop rules.)

Express your result in terms of given quantities and constants (ρ, ε, A, L). (Hint: Resistance is related to resistivity.)

i) $\frac{1}{R_{yz}} = \frac{1}{R_y} + \frac{1}{R_z} \Rightarrow R_{yz} = \frac{R_y R_z}{R_y + R_z} \Rightarrow R_{eq} = R_x + R_{yz} = R_x + \frac{R_y R_z}{R_y + R_z}$
 where $R_x = R_y = \rho \frac{L}{A}$ & $R_z = 3\rho \frac{L}{A} \Rightarrow R_{eq} = \rho \frac{L}{A} + \frac{\rho \frac{L}{A} \cdot 3\rho \frac{L}{A}}{\rho \frac{L}{A} + 3\rho \frac{L}{A}}$
 $\Rightarrow R_{eq} = \frac{7\rho L}{4A}$

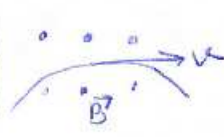
$i = \frac{\varepsilon}{R_{eq}} = \frac{4\varepsilon A}{7\rho L} = i_x$

ii) $i_x = i_y + i_z$

② loop 1: $\varepsilon - i_x R_x - i_y R_y = 0 \Rightarrow i_y = \frac{\varepsilon - i_x R_x}{R_y}$
 ② loop 2: $+i_y R_y - i_z R_z = 0 \Rightarrow i_z = i_y \frac{R_y}{R_z} = \left(\frac{\varepsilon - i_x R_x}{R_y}\right) \frac{R_y}{R_z}$
 $V = i_z R_z = \frac{\varepsilon - i_x R_x}{R_z} R_z = \varepsilon - i_x R_x$
 $= \varepsilon - \left(\frac{4\varepsilon A}{7\rho L}\right) \rho \frac{L}{A} = \varepsilon - \frac{4\varepsilon}{7} = \frac{3\varepsilon}{7}$

3. A proton of kinetic energy 2.10 keV circles in a plane perpendicular to a uniform magnetic field. The orbit radius is 25.0 cm. Find
- the proton's speed,
 - the magnetic field magnitude,
 - the circling frequency,
 - the period of the motion.

proton

$$\begin{cases}
 m \frac{v^2}{R} = qvB \sin 90 \\
 v = \frac{qRB}{m} \Rightarrow R = \frac{mv}{qB}
 \end{cases}$$


i) $\frac{1}{2} m_p v^2 = 2.1 \times 10^3 \text{ eV} \Rightarrow v^2 = \frac{2(2.1 \times 10^3 \text{ eV})(1.6 \times 10^{-19} \text{ J/eV})}{1.67 \times 10^{-27} \text{ kg}}$

$$\Rightarrow v = \boxed{0.634 \times 10^6 \text{ m/s}} \quad (3)$$

ii) $B = \frac{m_p v}{qR} = \frac{(1.67 \times 10^{-27} \text{ kg})(0.634 \times 10^6 \text{ m/s})}{(1.6 \times 10^{-19} \text{ C})(25 \times 10^{-2} \text{ m})} = \boxed{0.027 \text{ T}} \quad (3)$

iii) $T = \frac{1}{f} = \frac{2\pi R}{v} \Rightarrow f = \frac{v}{2\pi R} = \frac{0.634 \times 10^6 \text{ m/s}}{2\pi(25 \times 10^{-2} \text{ m})} = \boxed{0.404 \times 10^6 \text{ Hz}} \quad (2)$

iv) $T = \frac{1}{f} = \boxed{2.48 \times 10^{-6} \text{ s}} \quad (2)$

4. A long wire carries a 10 A current from left to right. An electron 1.0 cm above the wire is traveling to the right at a speed of 1.0×10^7 m/s. What are the magnitude and the direction of the magnetic force on the electrons?

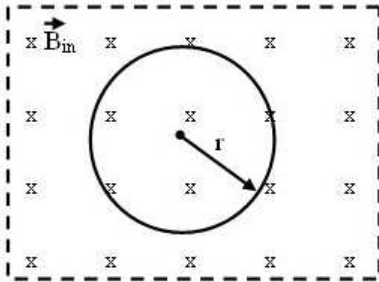
$$B = \frac{\mu_0 I}{2\pi d} = \frac{(4\pi \times 10^{-7} \text{ Tm/A}) 10 \text{ A}}{2\pi 1.0 \times 10^{-2} \text{ m}} = 2 \times 10^{-4} \text{ T}$$

$$\vec{F}_B = q \vec{v} \times \vec{B} \Rightarrow |\vec{F}_B| = (1.602 \times 10^{-19} \text{ C})(1.0 \times 10^7 \text{ m/s})(2 \times 10^{-4} \text{ T})$$

$$= 3.2 \times 10^{-16} \text{ N}$$

$$\vec{F}_B = 3.2 \times 10^{-16} \text{ N } \hat{j}$$

5. In figure below, the magnetic flux through the circular loop of radius $r = 2.0 \text{ m}$ increases according to the relation $\Phi_B = 6t^2 + 6t$, where Φ_B is in Webers and t is in seconds.



- Find the magnitude of the induced emf, ξ in the circular loop at $t = 2.0 \text{ s}$.
- What is the magnitude and direction of the induced current in the circular loop at $t = 2.0 \text{ s}$ if the loop has a total resistance of $R = 60 \Omega$?

i) $\phi_B(t) = 6t^2 + 6t$; increasing flux \Rightarrow induced \mathcal{E}, i should oppose

$$\mathcal{E} = -N \frac{d\phi_B}{dt} \Rightarrow |\mathcal{E}| = \frac{d(6t^2 + 6t)}{dt} \Big|_{t=2s} = 12t + 6 \Big|_{t=2s}$$

$\Rightarrow \mathcal{E} \Big|_{t=2s} = \underline{30 \text{ Volt}}$

ii) $i_{induced} = \frac{\mathcal{E}}{R} = \frac{30 \text{ Volt}}{60 \Omega} = 0.5 \text{ A}$

direction \rightarrow ccw

The diagram shows the circular loop with induced current $i_{induced}$ flowing counter-clockwise. The induced magnetic field $B_{induced}$ is shown as a grid of 'o' marks pointing out of the page, opposing the original field.