1 Approximation of Functions, Fourier Series

To construct the trigonometric polynomial of order M of the form

$$f(x) = \frac{A_0}{2} \sum_{j=1}^{M} [A_j \cos(jx) + B_j \sin(jx)]$$

based on the N equally spaced values $x_k = -\pi + 2\pi k/N$, for k = 1, 2, ..., N. The construction is possible provided that $2M + 1 \leq N$.

The following program constructs vectors A and B that contain the coefficients A_j and B_j , respectively, of the equation above of order M.

```
function [A,B]=tpcoeff(X,Y,M)
%Input
          - X is a vector of equally spaced abscisssas in [-pi, pi]
%
          - Y is a vector of ordinates
%
          - M is the degree of the trigomometric polynomial
%Output
          - A is a vector containing the coefficients of cos(jx)
%
          - B is a vector containing the coefficients of sin(jx)
N=length(X)-1;
\max 1 = fix((N-1)/2);
if M>max1
   M=max1;
end
A=zeros(1,M+1);
B=zeros(1,M+1);
Yends=(Y(1)+Y(N+1))/2;
Y(1)=Yends;
Y(N+1)=Yends;
A(1)=sum(Y);
for j=1:M
   A(j+1)=cos(j*X)*Y';
   B(j+1)=sin(j*X)*Y';
end
A=2*A/N;
B=2*B/N;
A(1)=A(1)/2;
```

You are given the function Y(X) = X for the interval $[-\pi, \pi]$.

1. Use the MATLAB program given above to calculate A_j s and B_j s. (**Hint:** You should first calculate all the Y values for a given M, say 100.) 2. The following program will evaluate the f(x) of order M at a particular value of x. A, B and M values are taken from the previous item.

```
function z=tp(A,B,x,M)
z=A(1);
for j=1:M
    z=z+A(j+1)*cos(j*x)+B(j+1)*sin(j*x);
end
```

Study the following commands:

>>x=-pi:.01:pi
>>y=tp(A,B,x,M)
>>plot(x,y,X,Y,'o')

3. Repeat the procedure for the *M*-values, 10, 20, 50. Compare the results Solution:

```
function calc(M)
X=-pi:.01:pi;
Y=X;
[A,B] = tpcoeff(X,Y,M);
x=-pi:.01:pi;
y=tp(A,B,x,M);
plot(x,y,X,Y,'-');
function drawer
ARR= [10,20,50,100];
len=length(ARR);
for i=1:len
    subplot(len,1,i)
    calc(ARR(i));
end
```

save with the names calc.m and drawer.m. Then;

>> drawer

This solution is supplied by Ömer Sezgin Uğurlu.

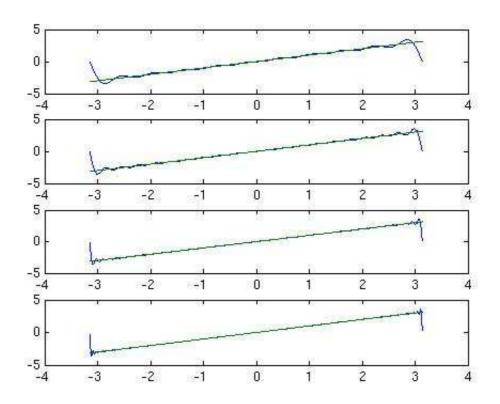


Figure 1: subplot(len,1,i).