

Chapter 1- Measurement

Measurements } Science & Engineering, So, how things are measured and compared.
 Comparisons } based on \Rightarrow experiments to establish the units for those measurements and comparisons.

measure the quantities: such as length, time, mass, temperature, pressure, electric current

in their own units (by comparison with a standard)

i.e. meter (m) for the quantity length. • standard corresponds to exactly 1.0 units of the quantity
 • standard for the length (1.0 m)
 \Rightarrow distance traveled by light in a vacuum during a certain fraction of a second.

So many physical quantities !! { not all independent } speed $\sim \frac{\text{length}}{\text{time}}$ } Becomes small number of physical quantities.

Units for three SI Base Quantities

Quantity	Unit Name	Unit Symbol
length	meter	m
Time	second	s
Mass	kilogram	kg

[L] [M] [T] Base quantities Base standards (Seven)

Derived Units:

Units are defined in terms of base units.

i.e. SI unit for power, Watt
 $1 \text{ Watt} = 1 \text{ W} = 1 \text{ kg} \frac{\text{m}^2}{\text{s}^3}$

SI Units \equiv Metric system

Example: Find the distance that light travels in one year.

$c = 2.998 \times 10^8 \text{ m/s}$ light year, ly
 Base Unit: time $1 = \frac{60 \text{ sec}}{1 \text{ min}}, 1 = \frac{365.25 \text{ day}}{1 \text{ year}}, 1 \text{ ly} = \frac{(2.998 \times 10^8 \text{ m/s})}{(\text{year})}$

$$1 \text{ ly} = (2.998 \times 10^8 \text{ m/s}) (1 \text{ year}) \left(\frac{365.25 \text{ day}}{1 \text{ year}} \right) \left(\frac{24 \text{ hours}}{1 \text{ day}} \right) \left(\frac{60 \text{ min}}{1 \text{ hour}} \right) \left(\frac{60 \text{ sec}}{1 \text{ min}} \right)$$

$$= 9.461 \times 10^{15} \text{ m}$$

Very large quantities; we need scientific notation \Rightarrow powers of 10
 Very small quantities; we need scientific notation \Rightarrow powers of 10

0.00035 $\xrightarrow{2 \sim \# \text{ of significant figures}}$ 3.5×10^{-4} or 3.5E^{-4} ; exponent of ten

0.000325400 $\xrightarrow{6}$ 3.25400×10^{-4}

2500 $\xrightarrow{2}$ 2.5×10^3

3560000000 $\xrightarrow{3}$ 3.56×10^9

10 sf? Do we know the quantity so accurate? Solution is the scientific notation.

See Table 1.2 for Prefixes for SI Units.

1.27×10^9 watts = 1.27 gigawatts = 1.27 GW

2.35×10^{-9} s = 2.35 nanosecond = 2.35 ns

See lecture notes for "Changing Units", Chain-link conversion

Example: Uncertainty, How accurate?

Page width? a measure: 1 mm divisions (accuracy)

21.6 cm

21.6 ± 0.1 cm

plus minus 0.1: Error in measurement

Percentage error in measurement: $\left(\frac{0.1}{21.6}\right) \times 100 = 0.5\%$

Page area?

21.6 cm (± 0.1)

27.9 cm (± 0.1)

(0.4%) what is the percentage error in measurement?

$(21.6 \text{ cm}) \times (27.9 \text{ cm}) = 603 \text{ cm}^2$
 what about uncertainty in measurement of area?

(0.4 + 0.5) addition 0.9 \rightarrow 0.9%

$(0.9) \times (603 \text{ cm}^2) = 5 \text{ cm}^2 \Rightarrow 603 \pm 5 \text{ cm}^2$

Example: Significant figures (sf) Physical properties \rightarrow uncertain

2.00 m (3 sf) \leftarrow OR \leftarrow 1.995 m ?

2.000 m (4 sf) \leftarrow 1.9995 m \leftarrow 2.0005 m

603 cm² (3 sf) \leftarrow 602.5 cm² \leftarrow 603.5 cm²

0.00035 (2 sf, not 6 sf)

mass of earth 5.98×10^{24} kg (3 sf)

6.0 $\times 10^{24}$ kg (2 sf)

In calculations, in exams!

$\frac{3.0}{11.0} = 0.27272727 \dots$ with calculator

\Rightarrow what should be the answer?!
 \Rightarrow least number of sf!

$\Rightarrow 0.27 \checkmark$